

Concurrent materials design

Gareth Conduit

Patent GB1302743.8 (2013)

Patent GB1307533.8 (2013)

Patent GB1307535.3 (2013)

Acta Materialia, **61**, 3378 (2013)

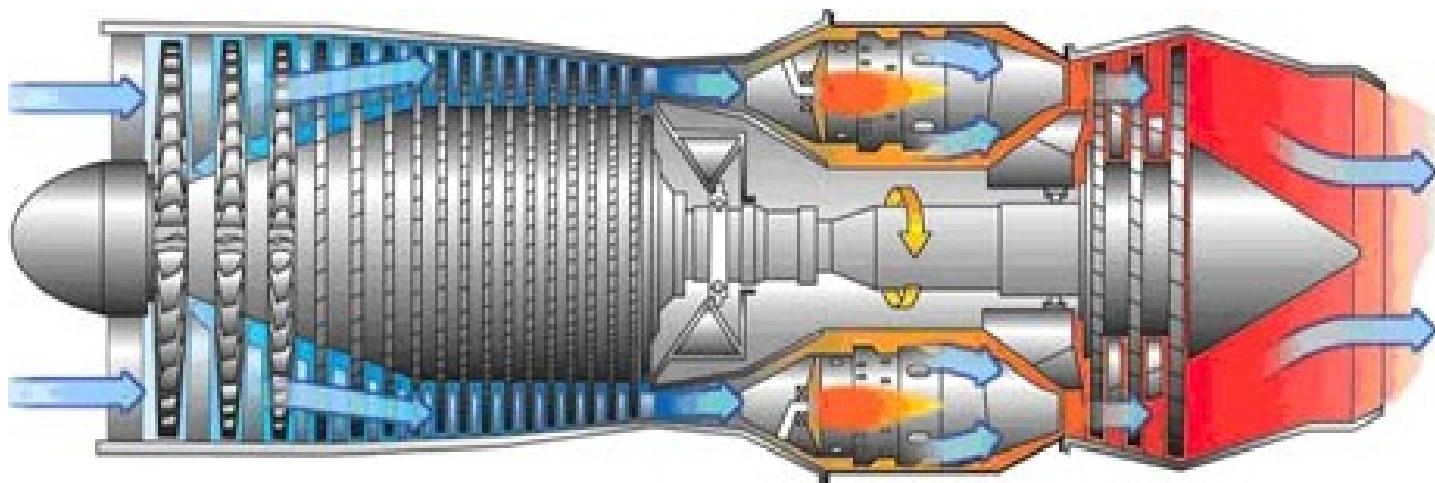
Submitted to Intermetallics (2013)

Rolls-Royce Group plc invention submission NC13006 (2013)

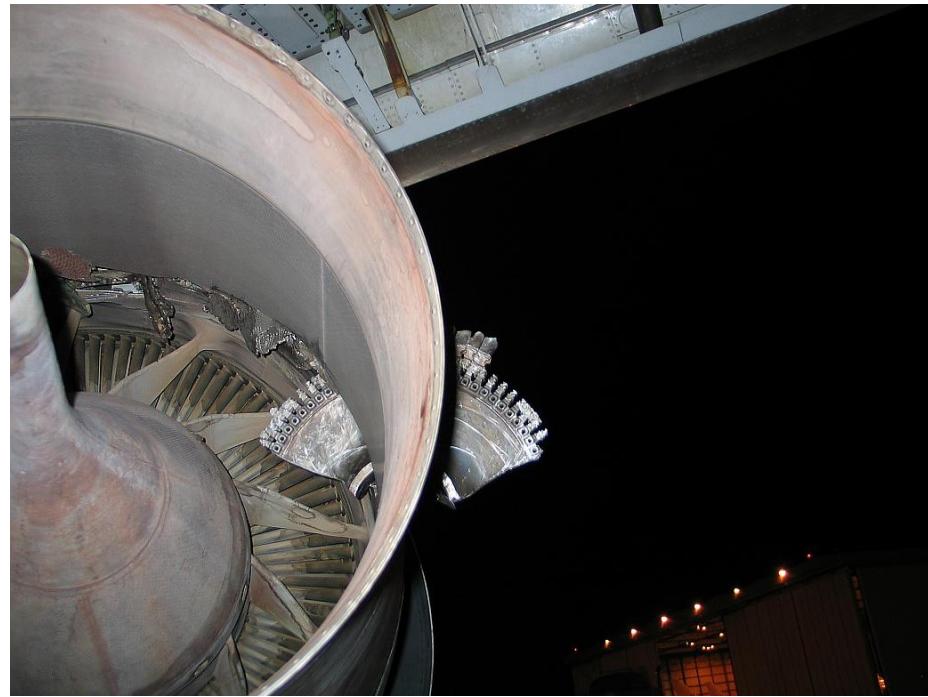
Rolls-Royce Group plc invention submission NC12261 (2012)

TCM Group, Department of Physics

Jet engine



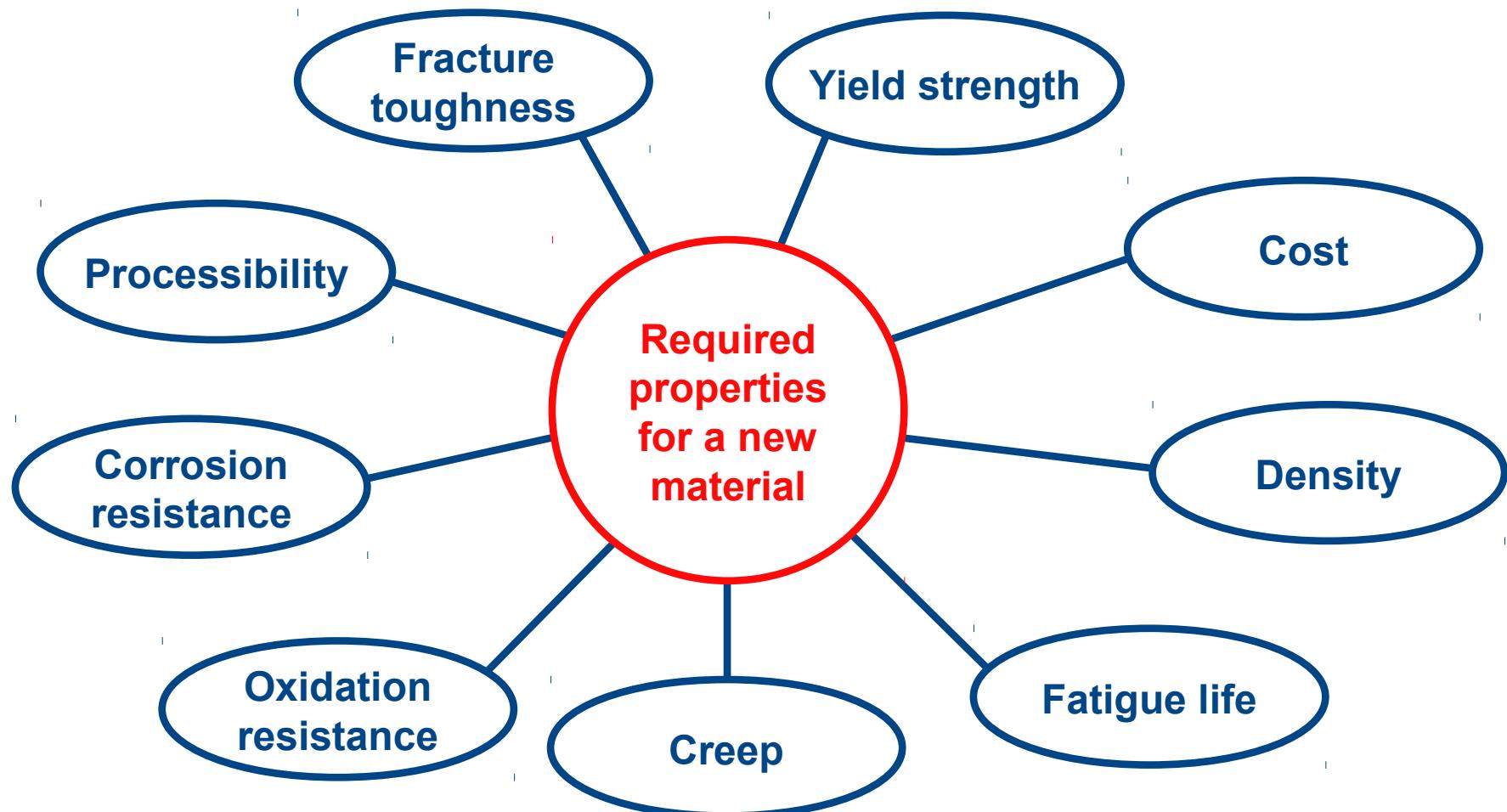
Jet engine: disc failure



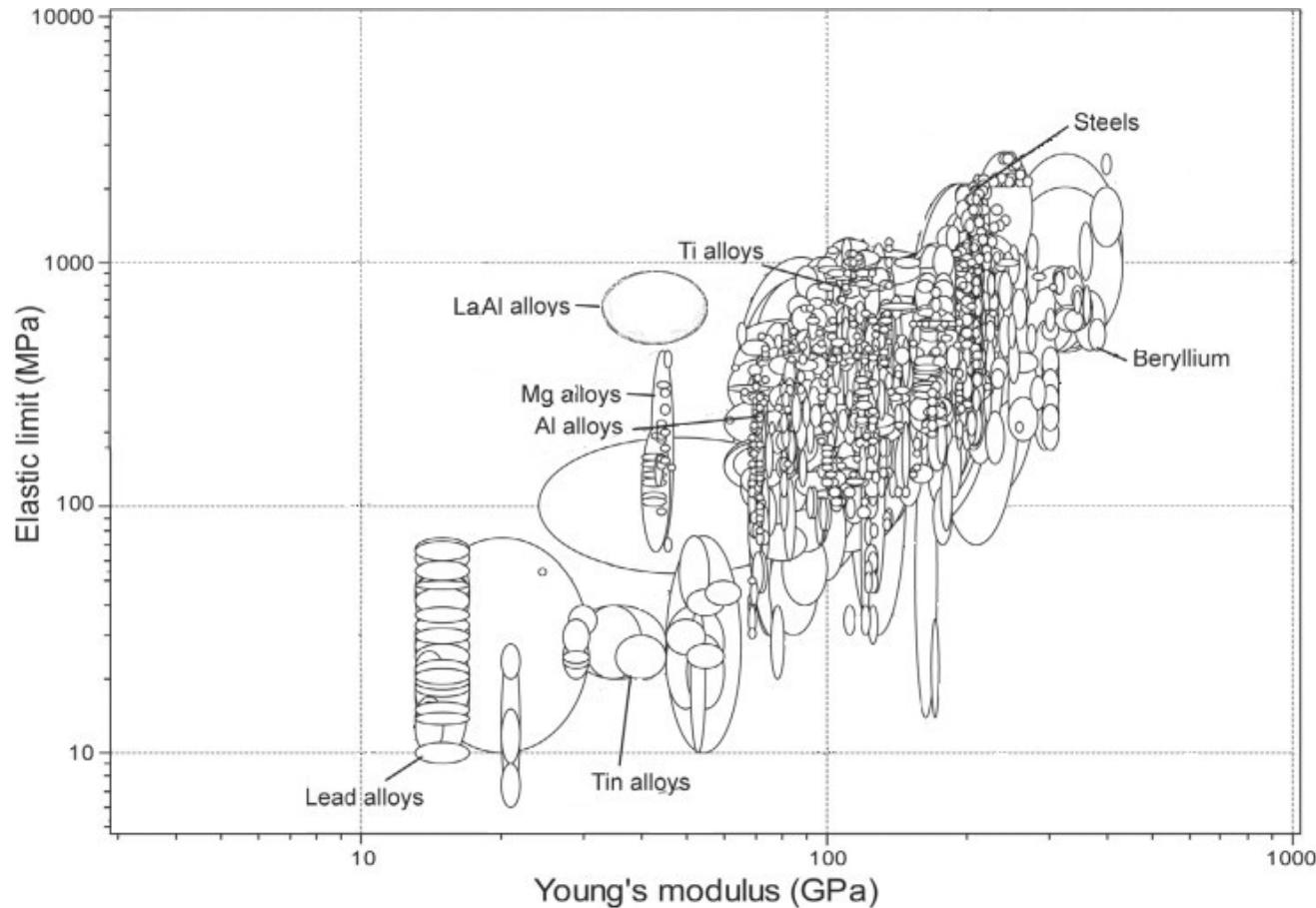
Jet engine: bird strike



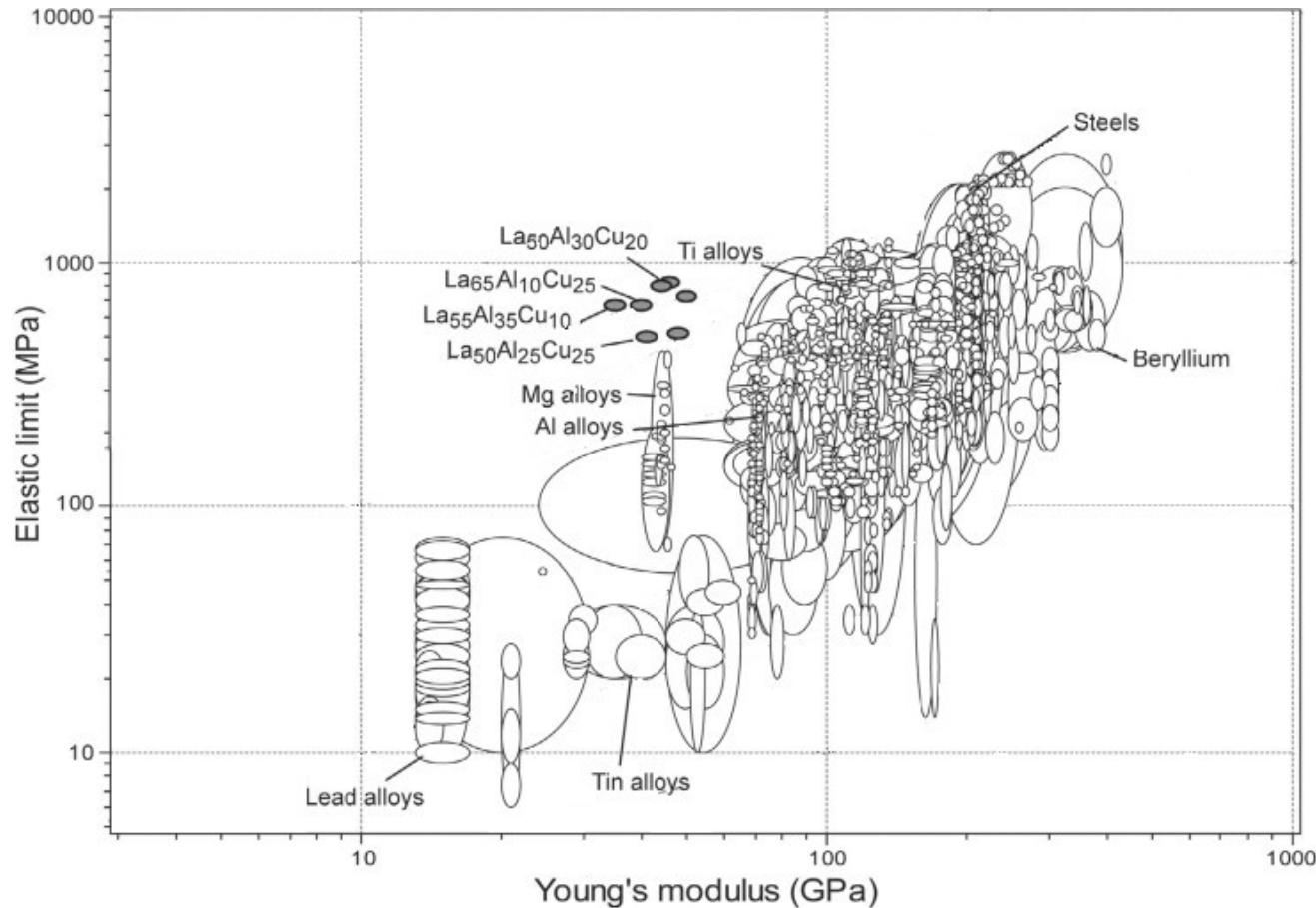
Designing a new material – what is required ?



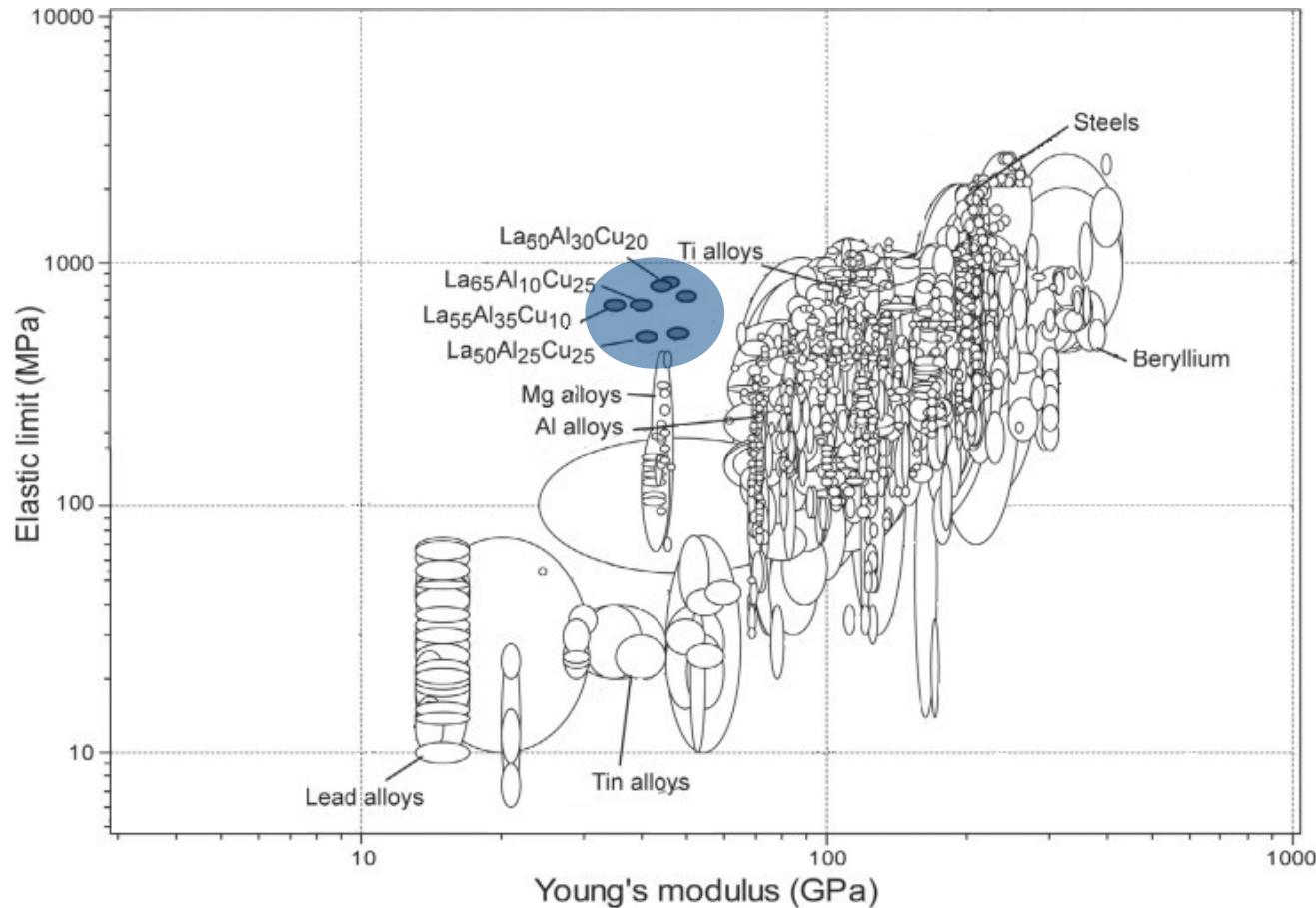
Materials selection



Materials selection



Materials selection



Materials selection

Guide the discovery of new materials

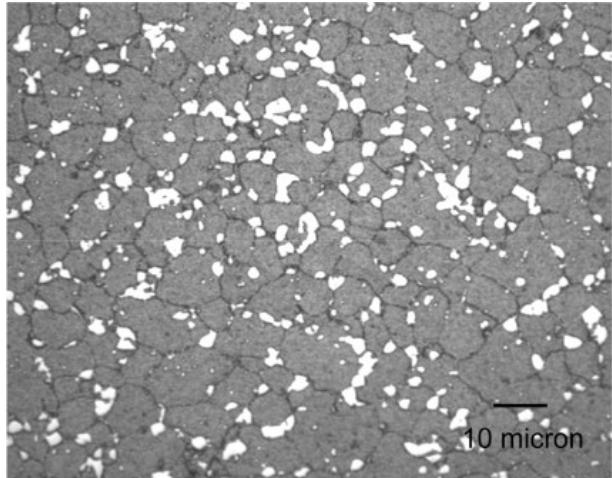
Concurrent materials design

Assess data quality

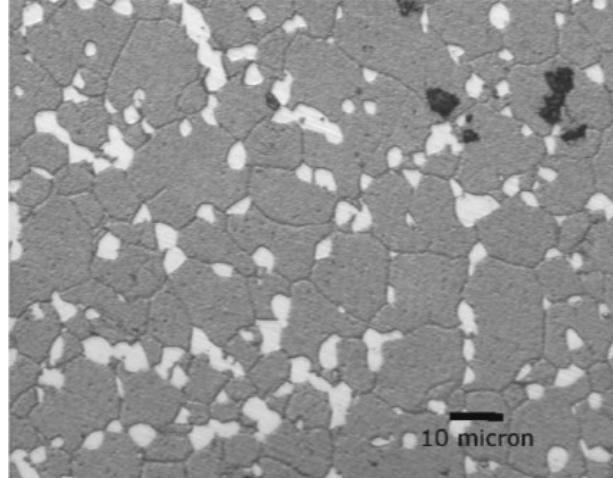
Estimate missing data

Contemporary alloys

RR1000

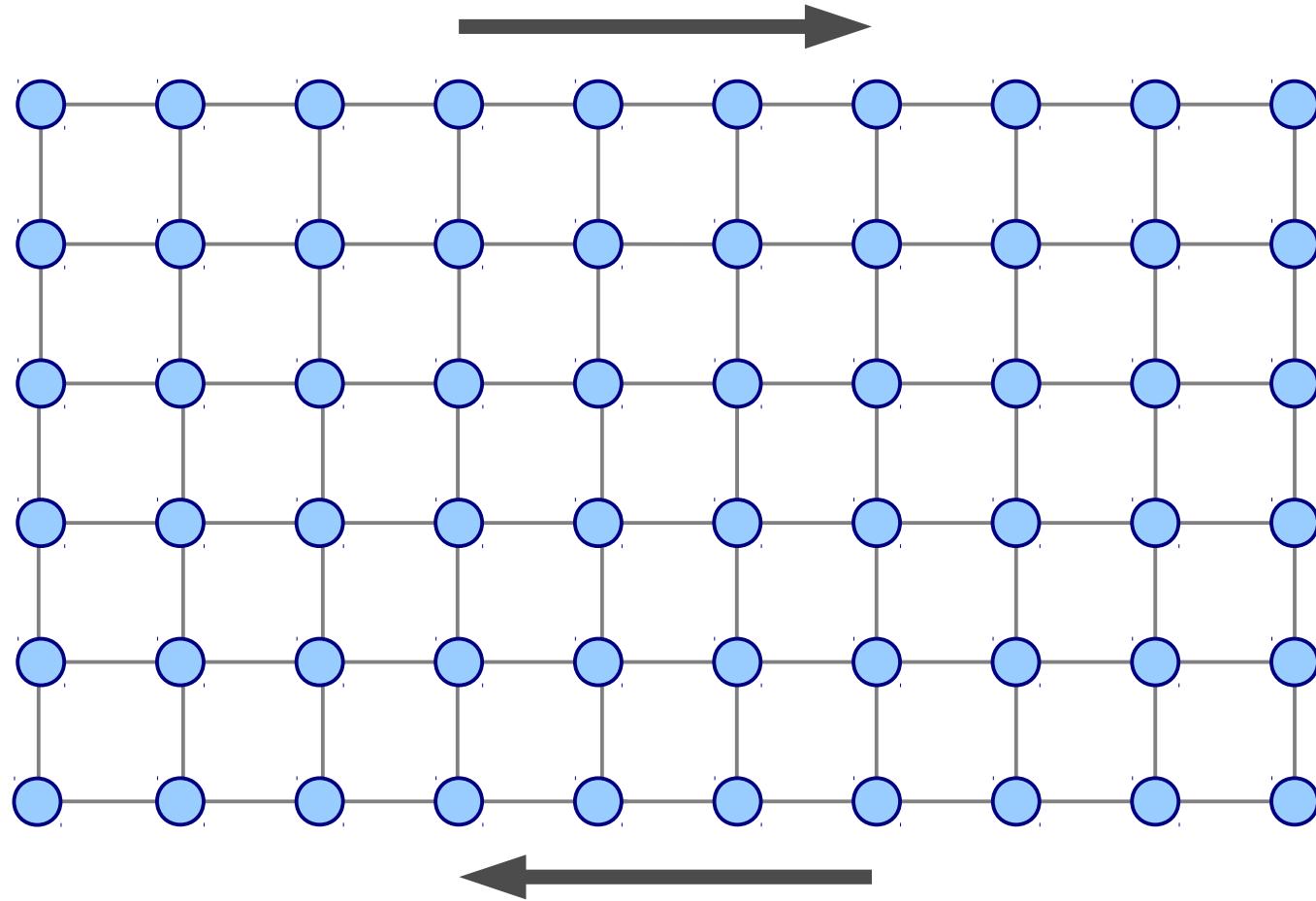


N18

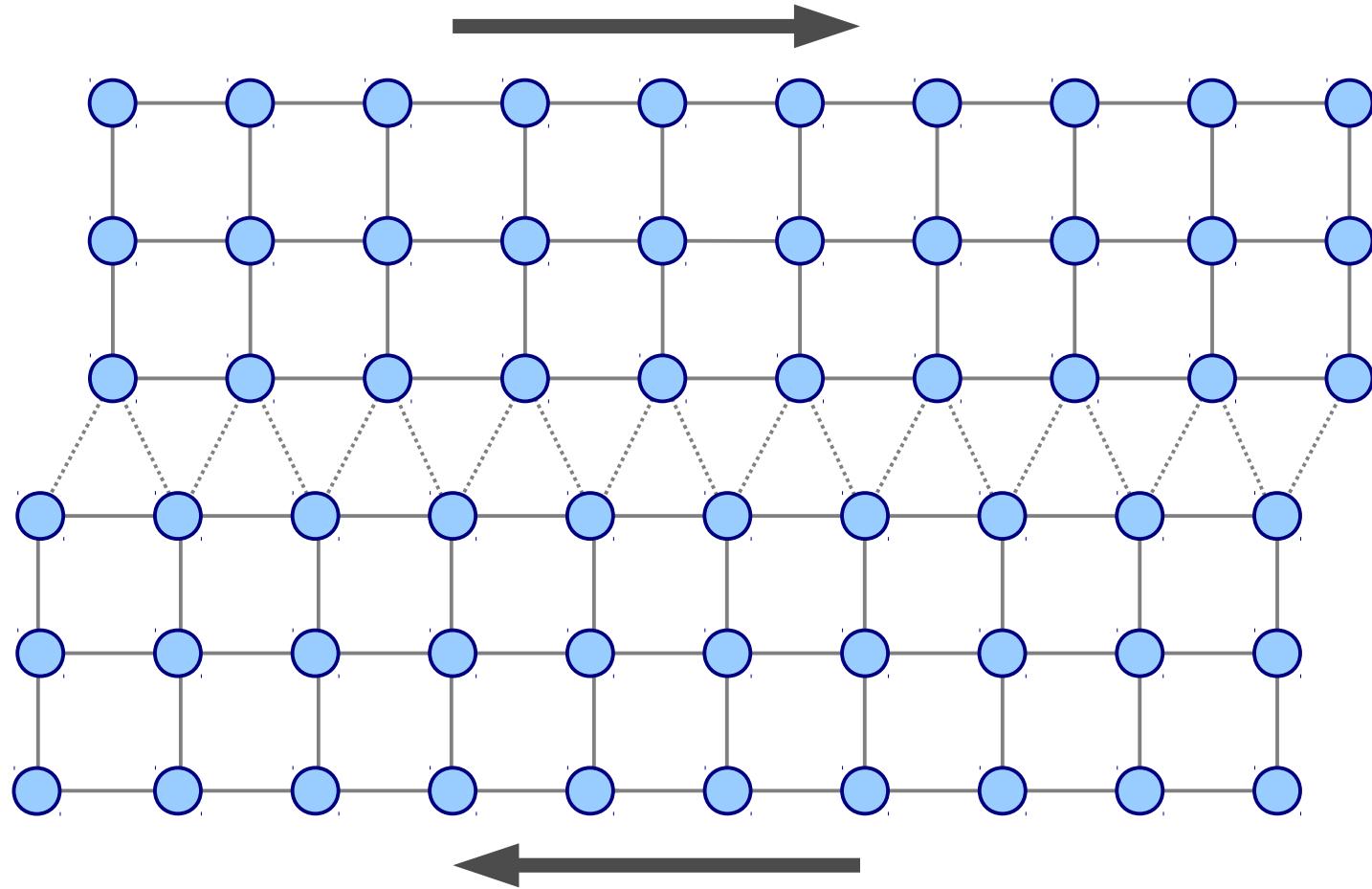


Alloy	Firm	Ni	Cr	Co	Mo	Ti	Al	C	Hf	Ta	W	Nb
Waspaloy	UTC	58	19	13	4	3	1.4					
N18	SNECMA	58	11.1	15.4	6.4	4.3	4.3	0.02	0.5			
Rene 88	General Elec.	56.5	16	13	4	3.7	2.1	0.03			4	0.7
RR1000	Rolls Royce	52.4	15	18.5	5	3.6	3	0.03	0.5	2		

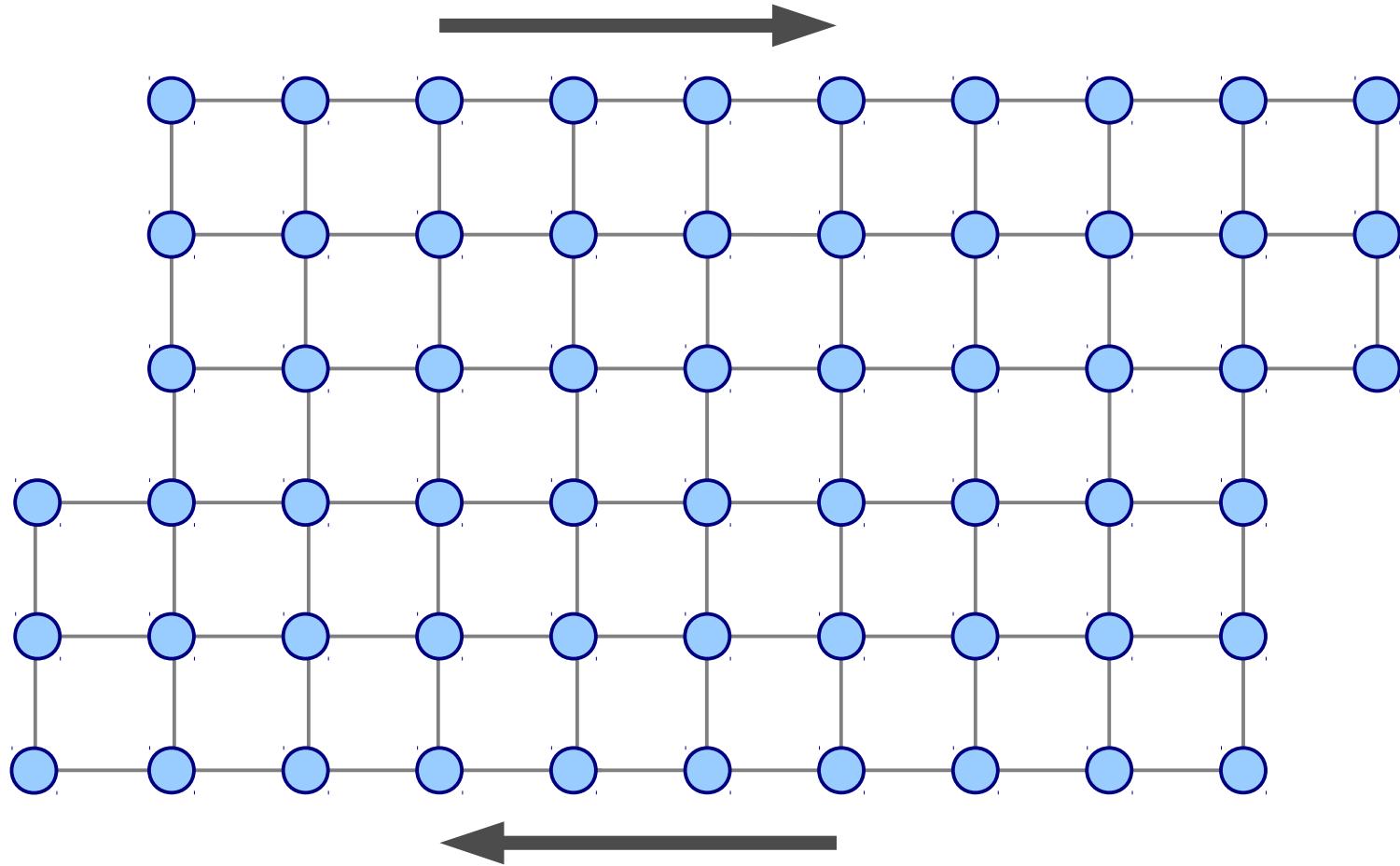
Creep



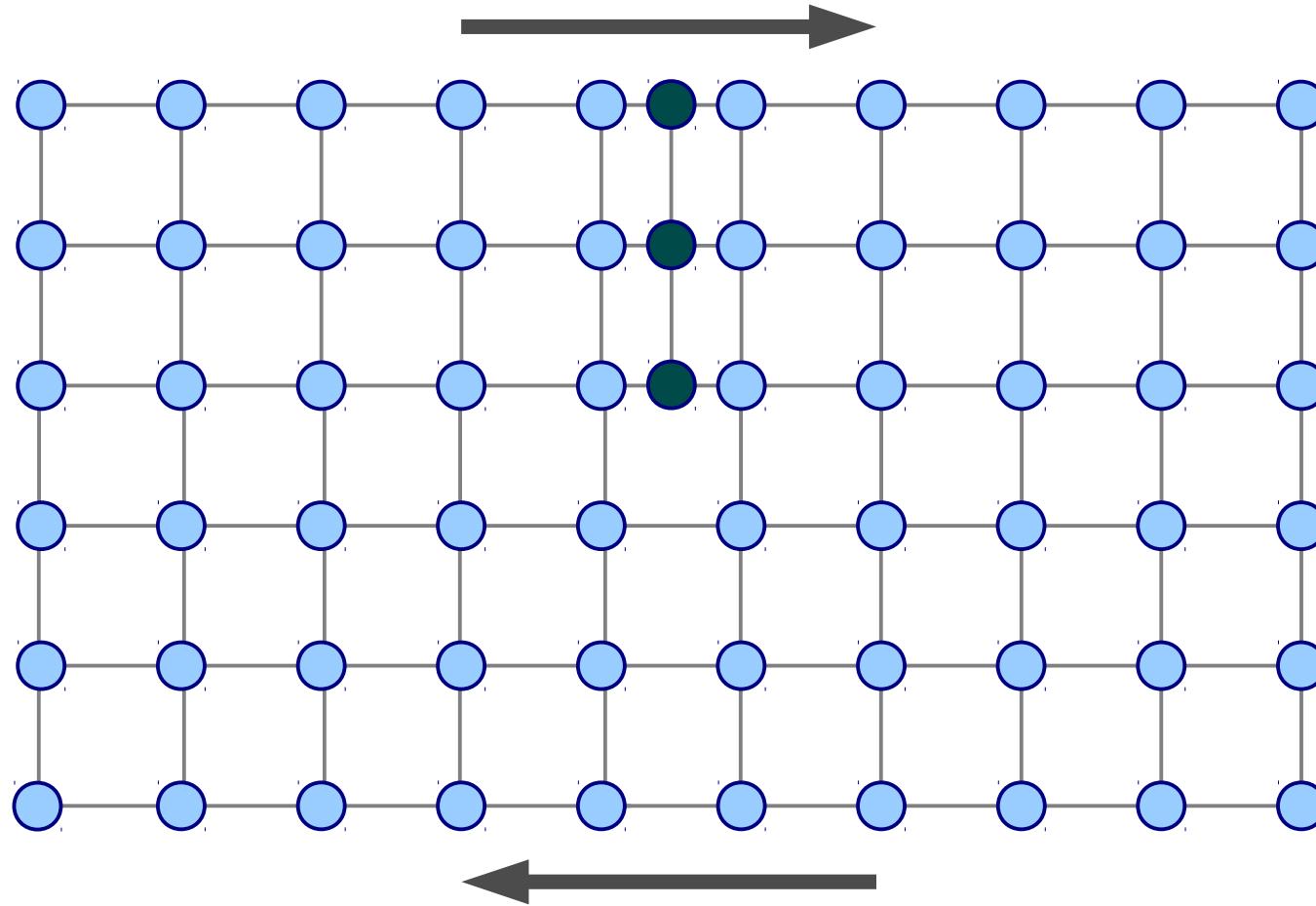
Creep



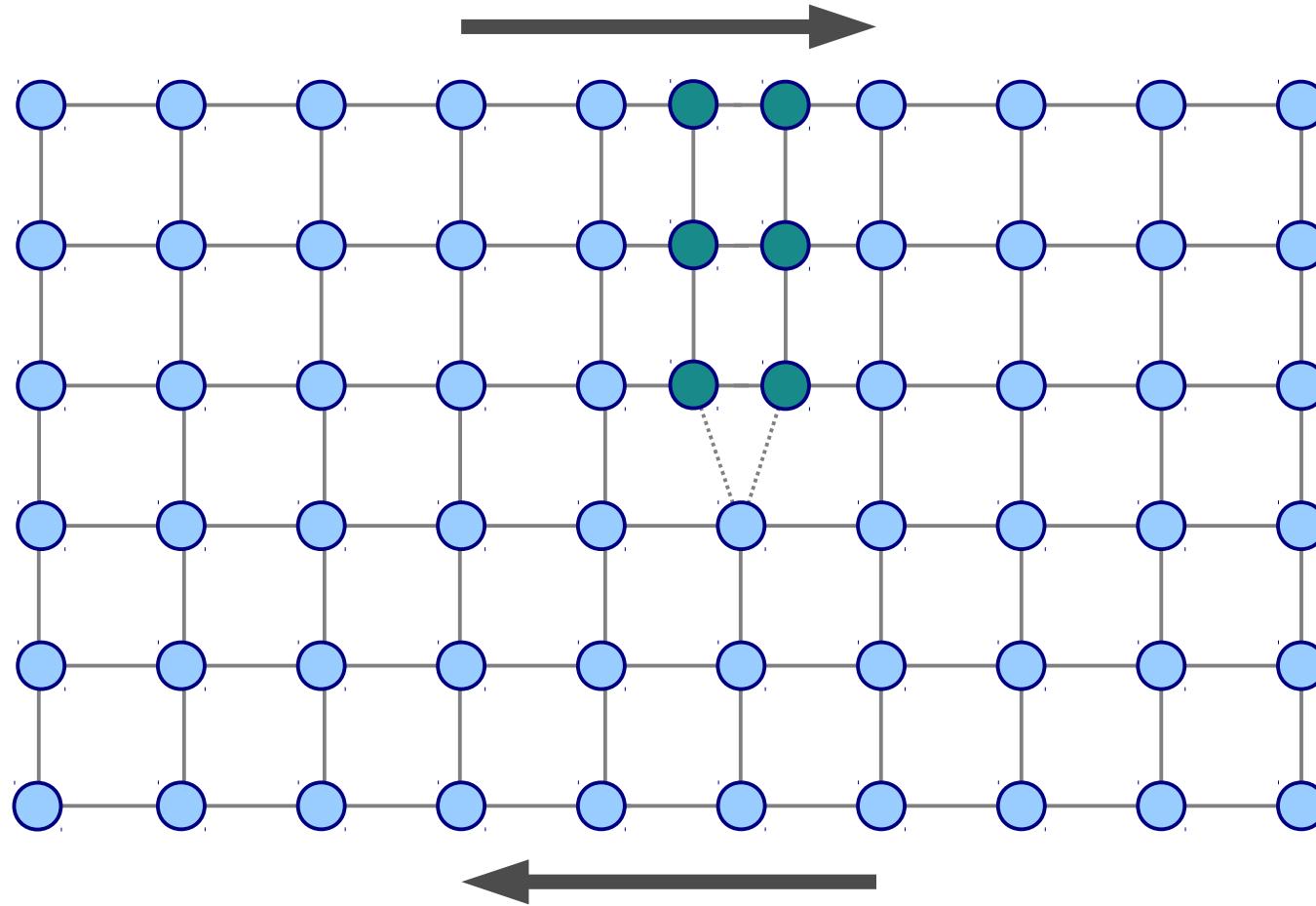
Creep



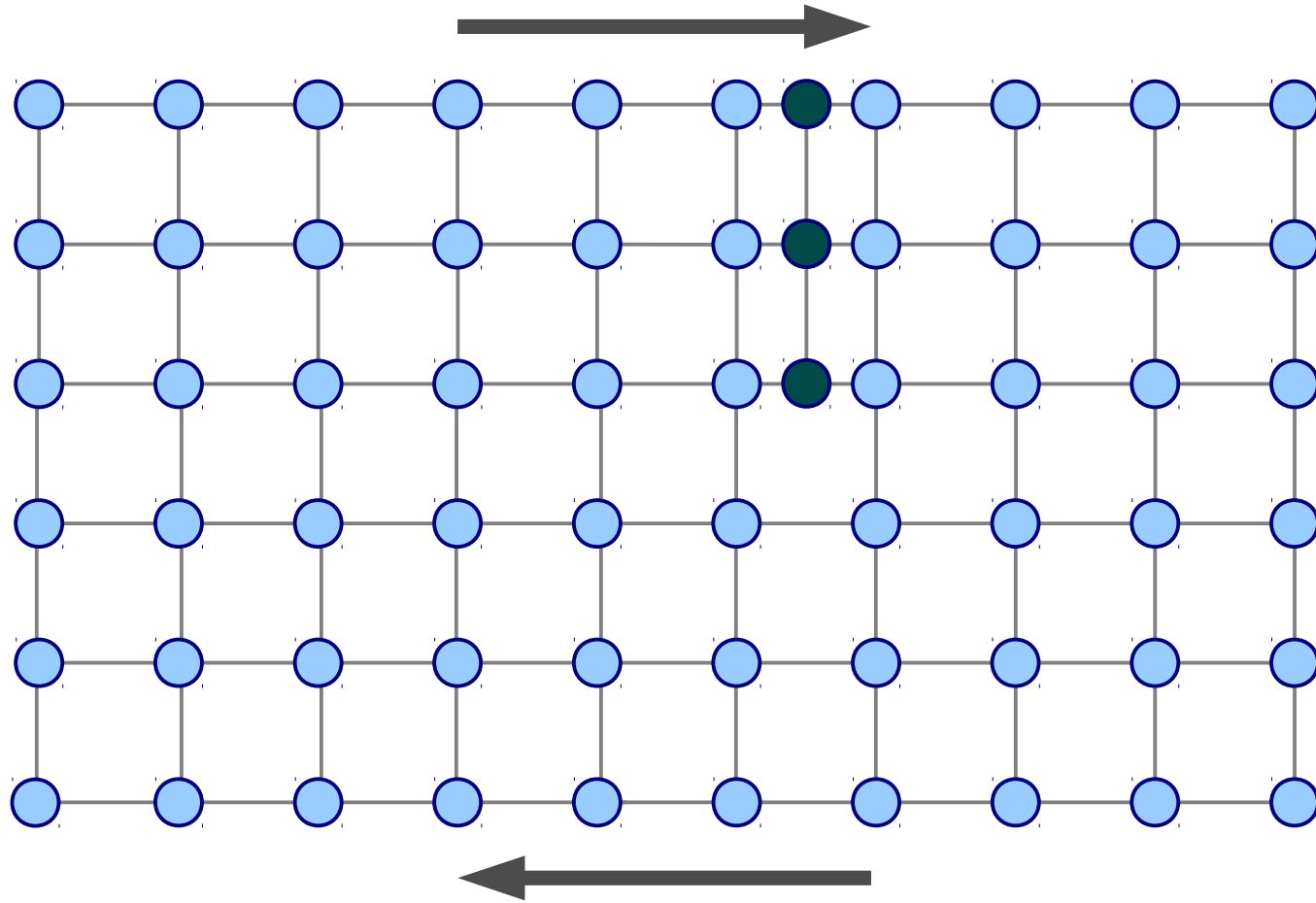
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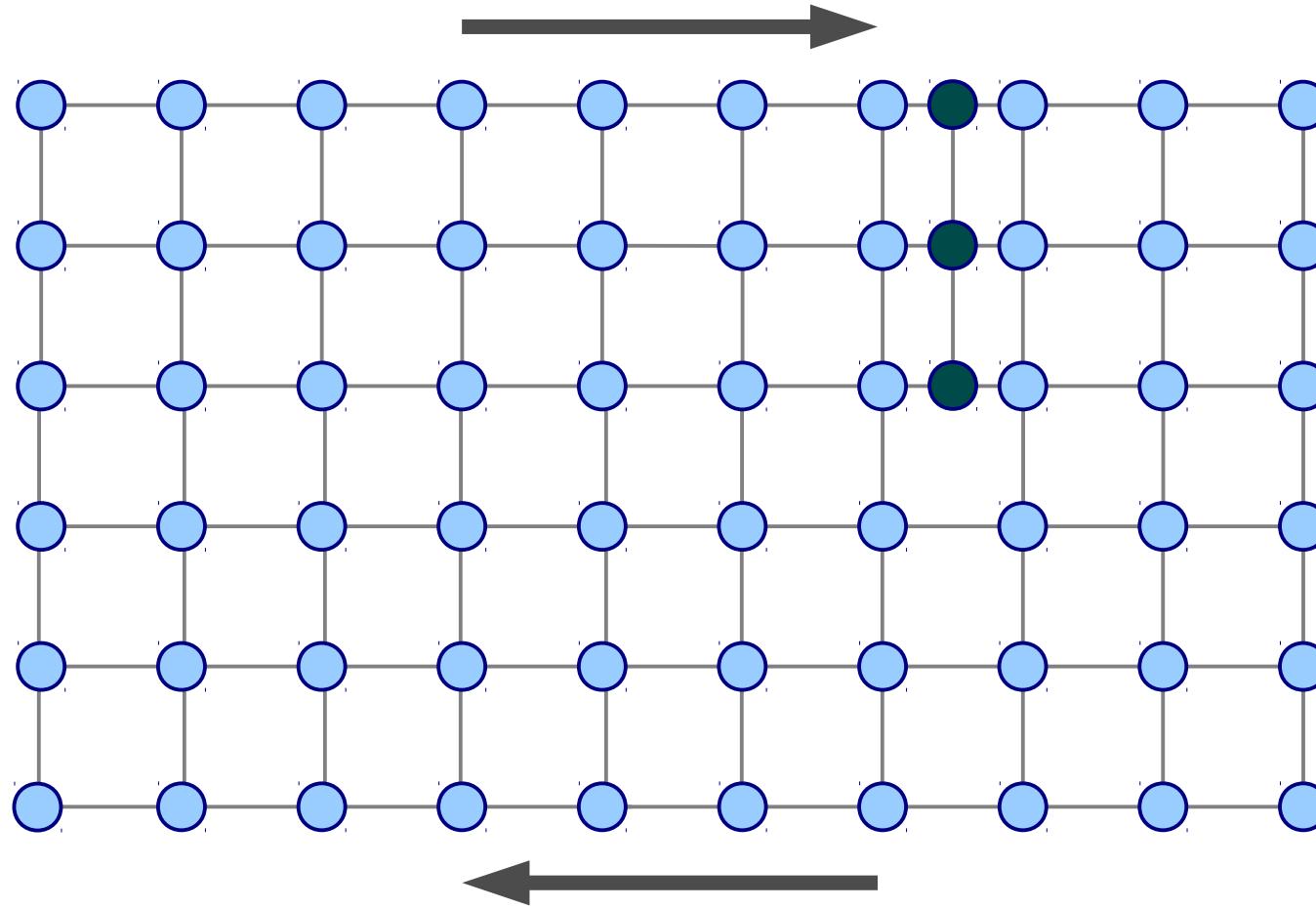
Creep



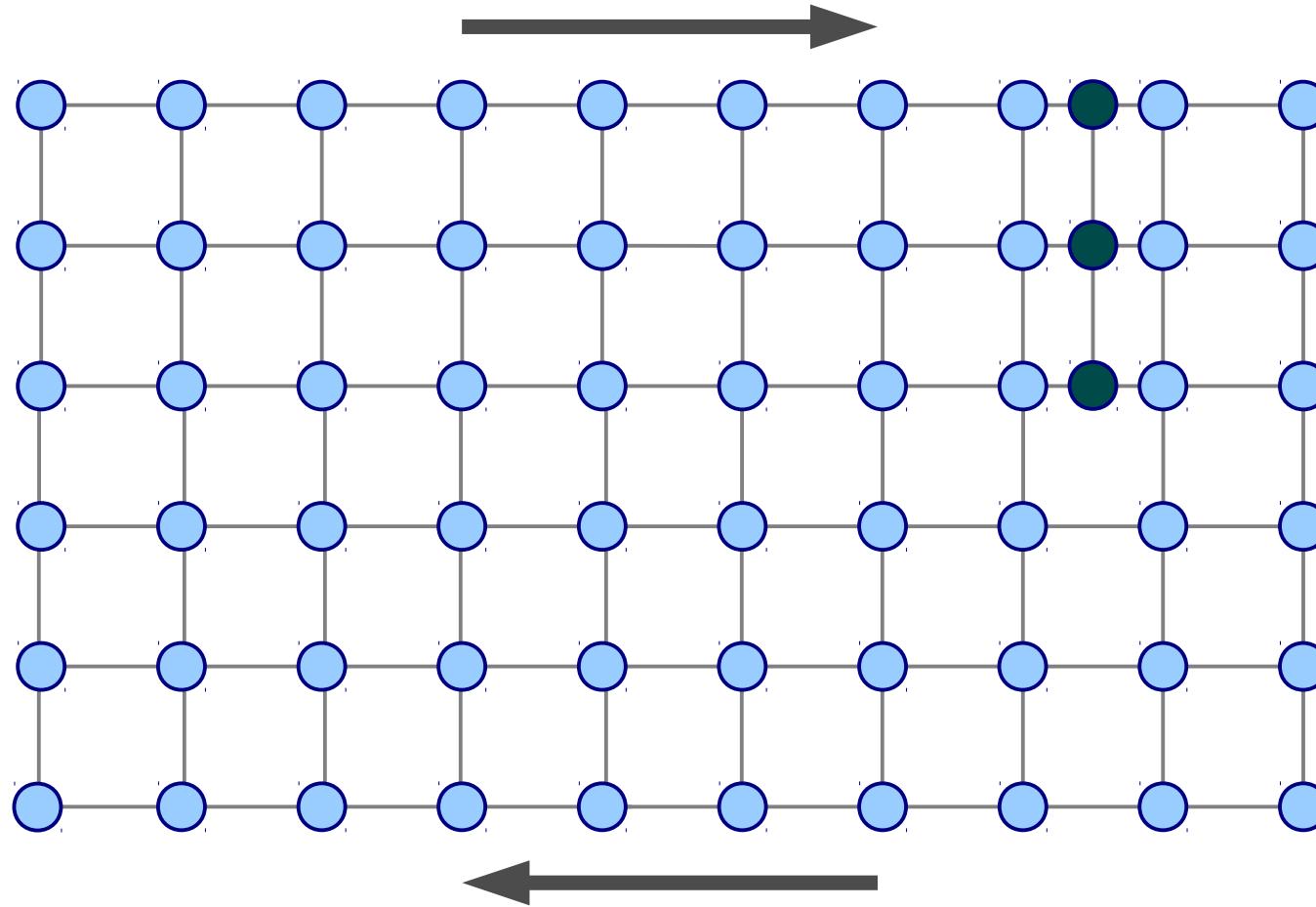
Creep



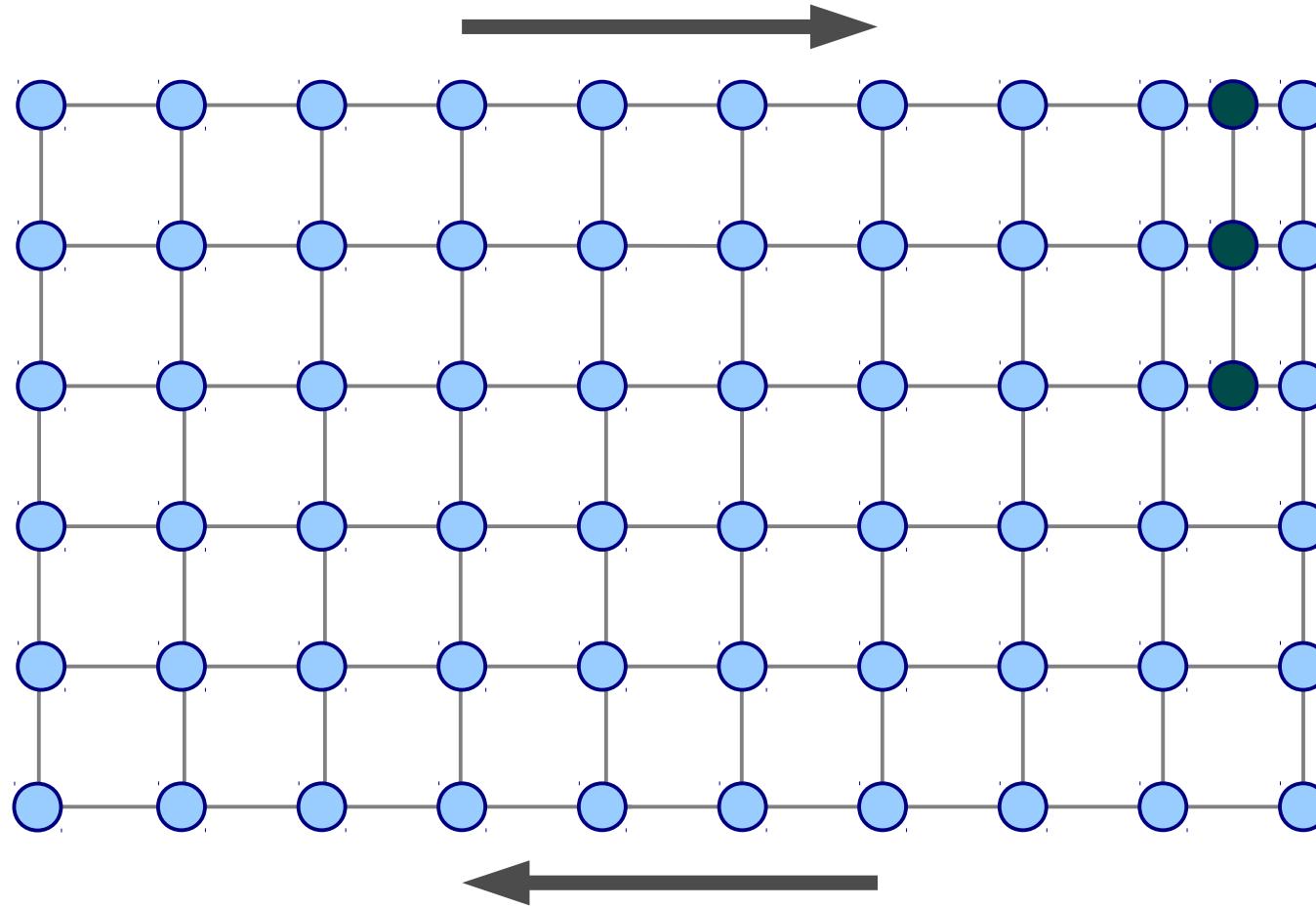
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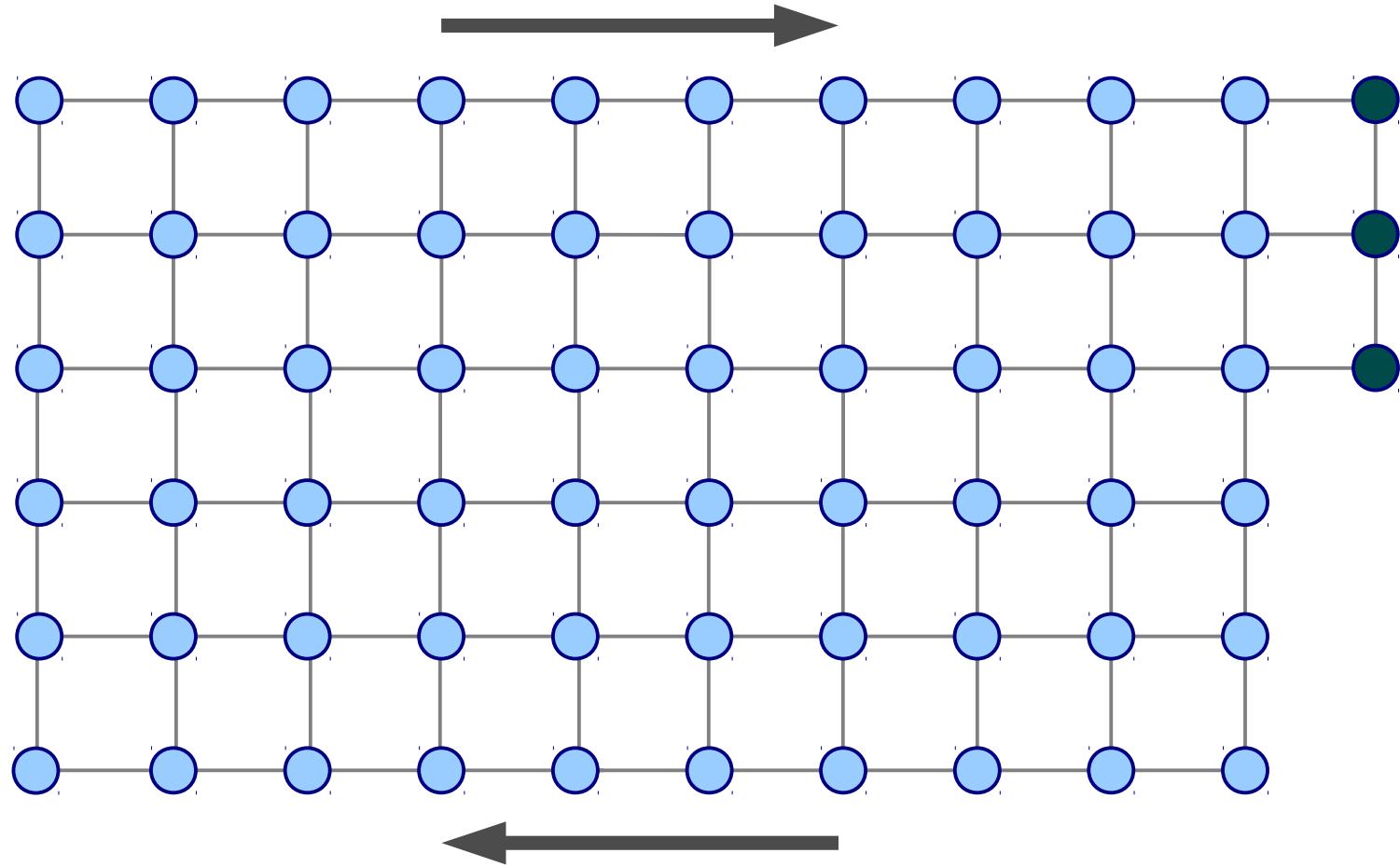
Creep



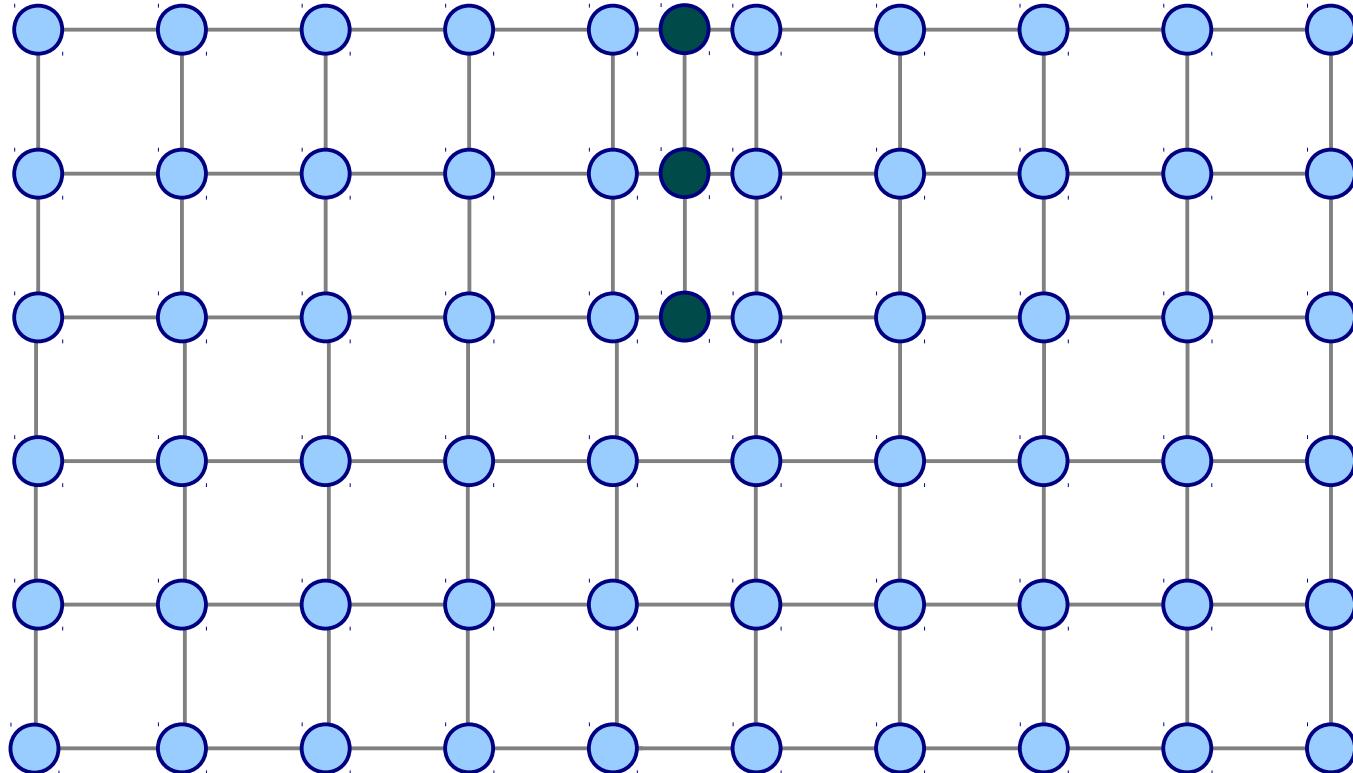
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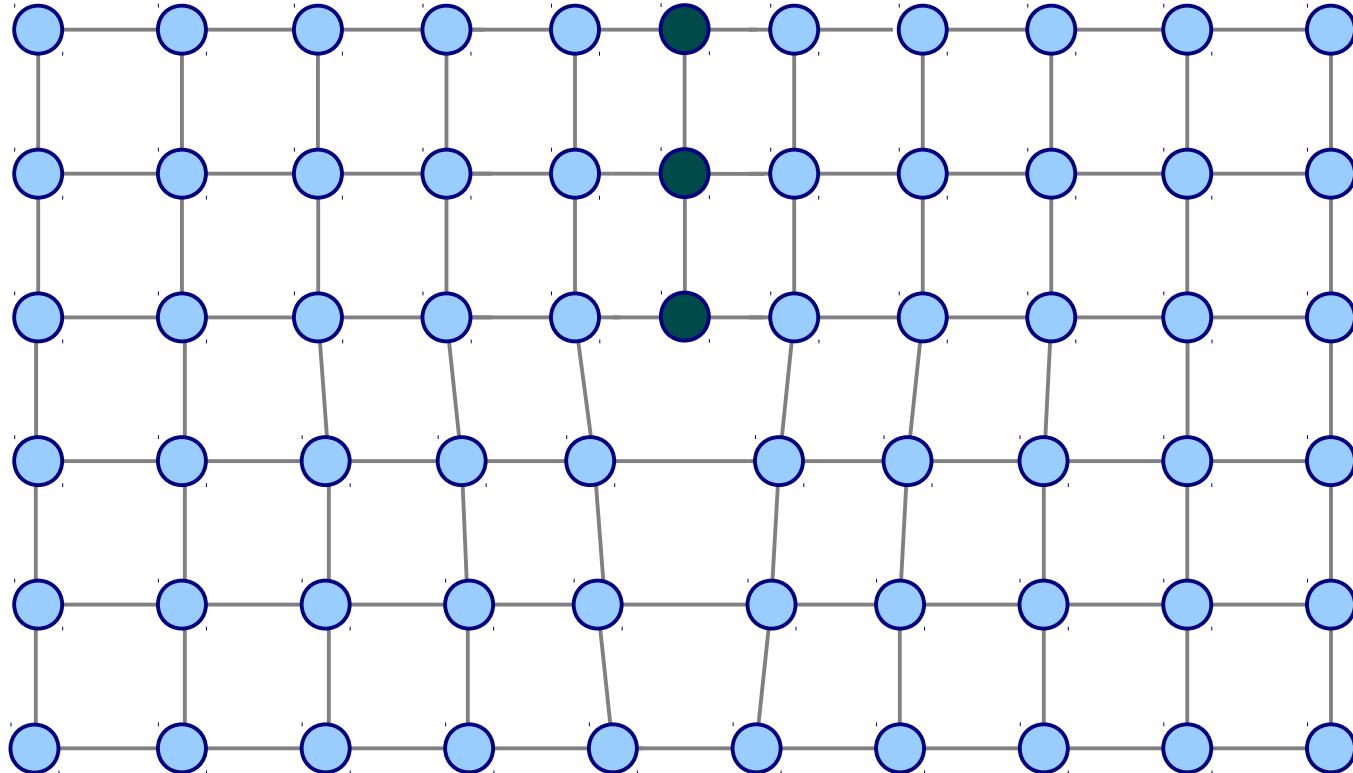
Creep



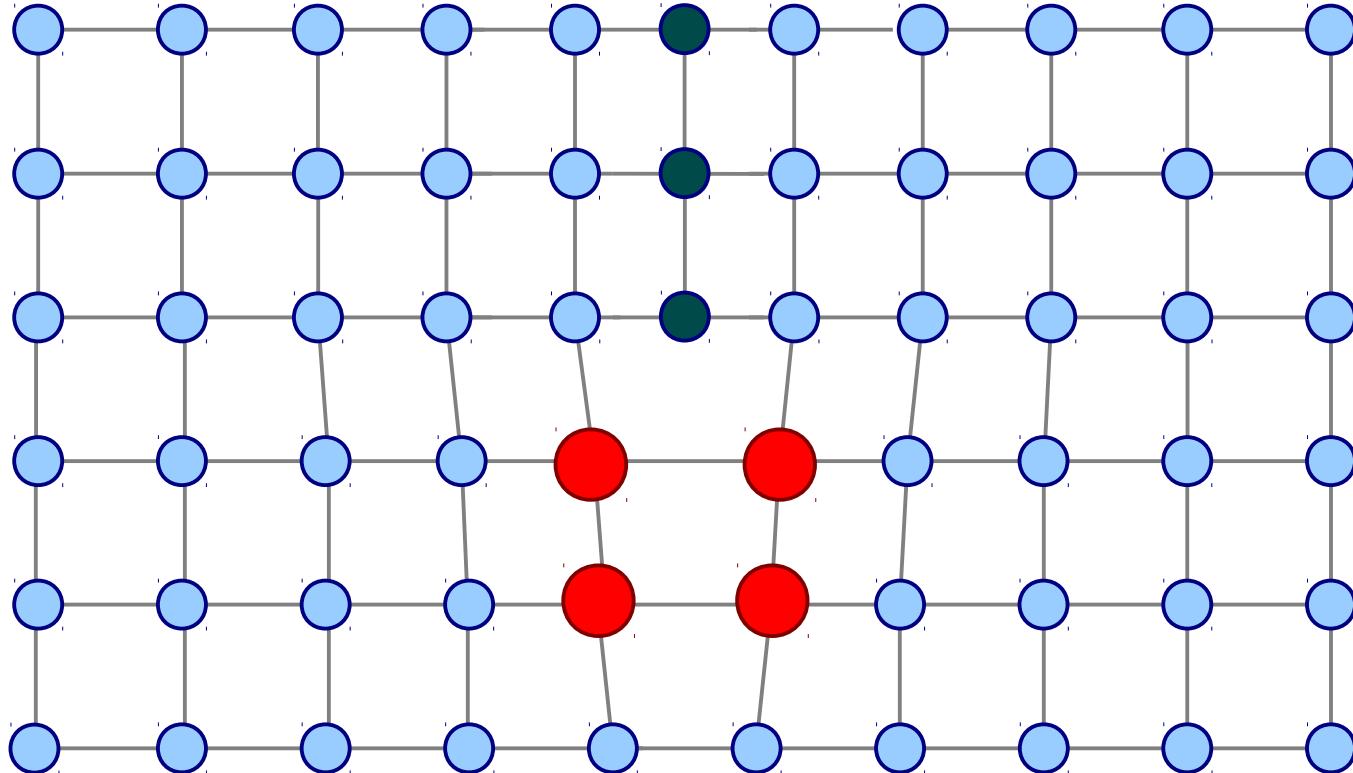
Solution hardening



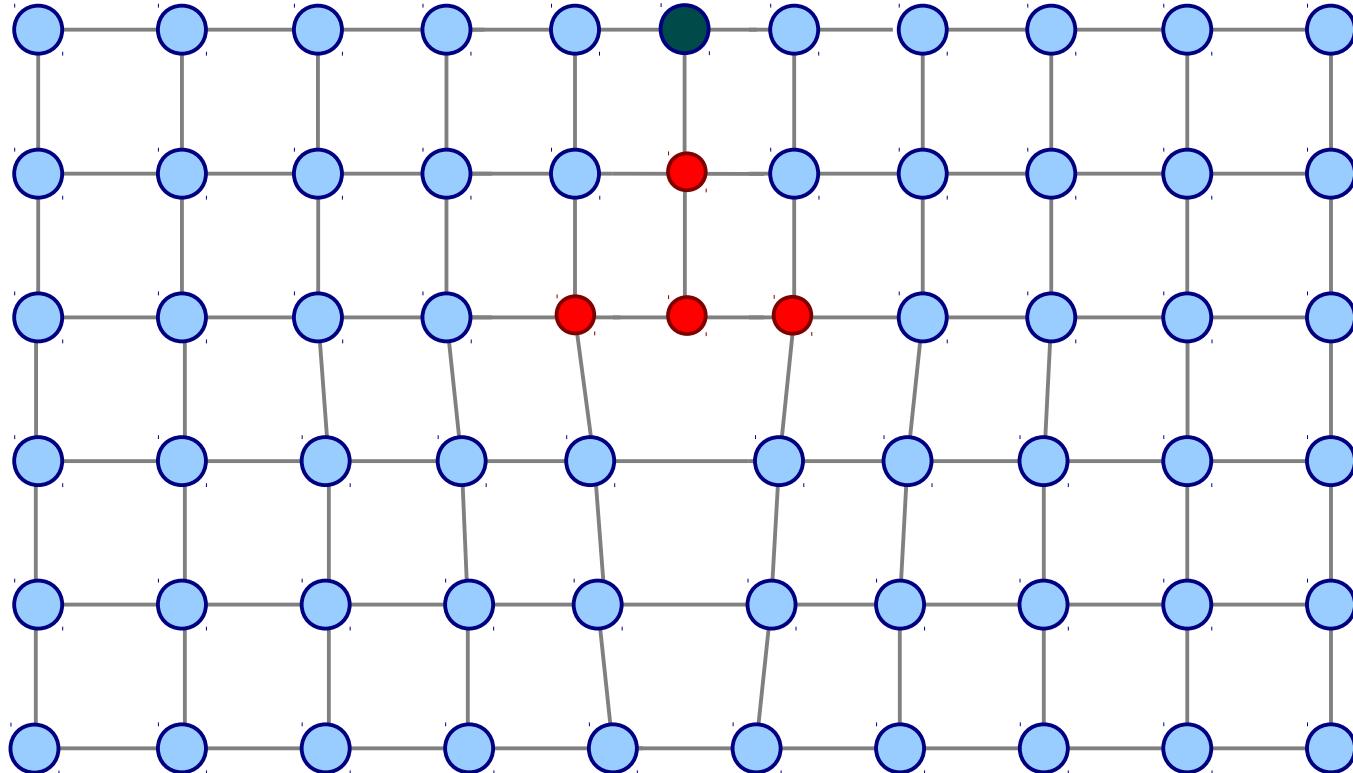
Solution hardening



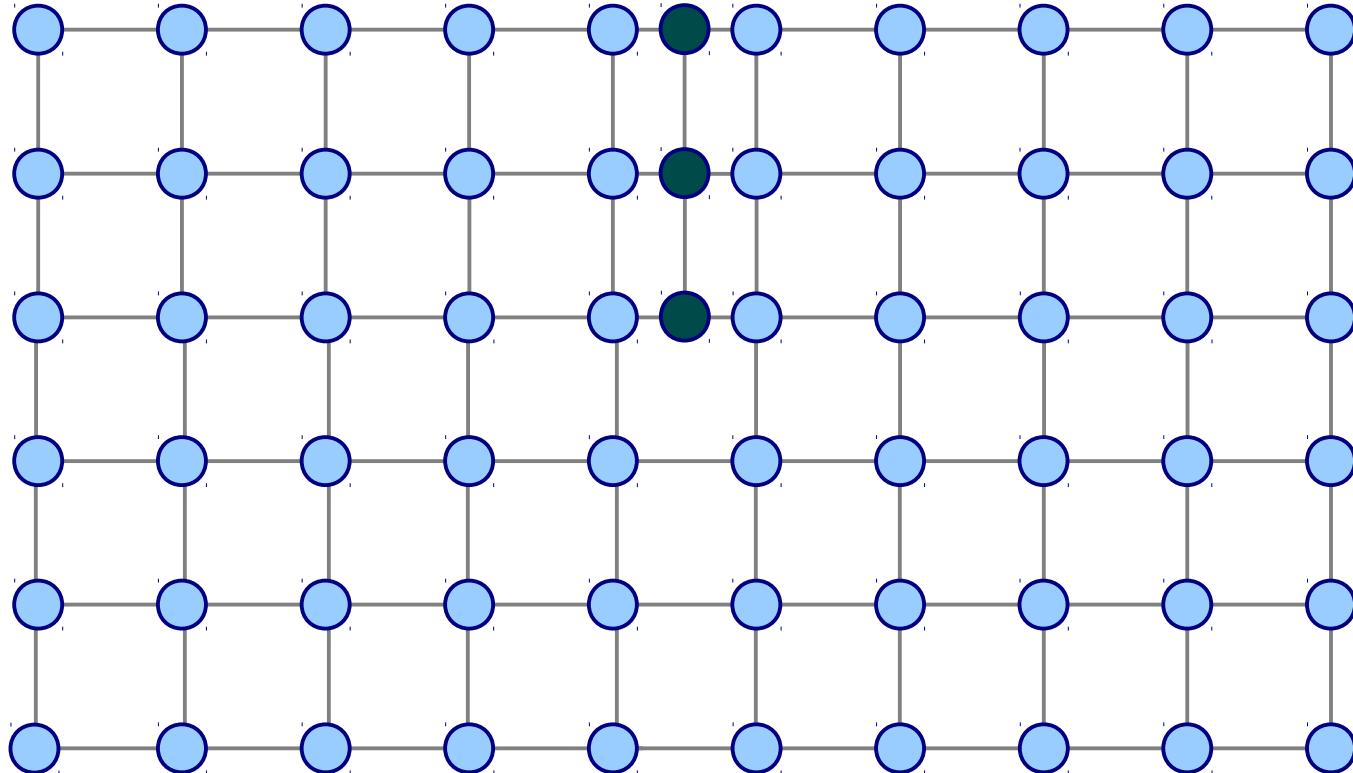
Solution hardening



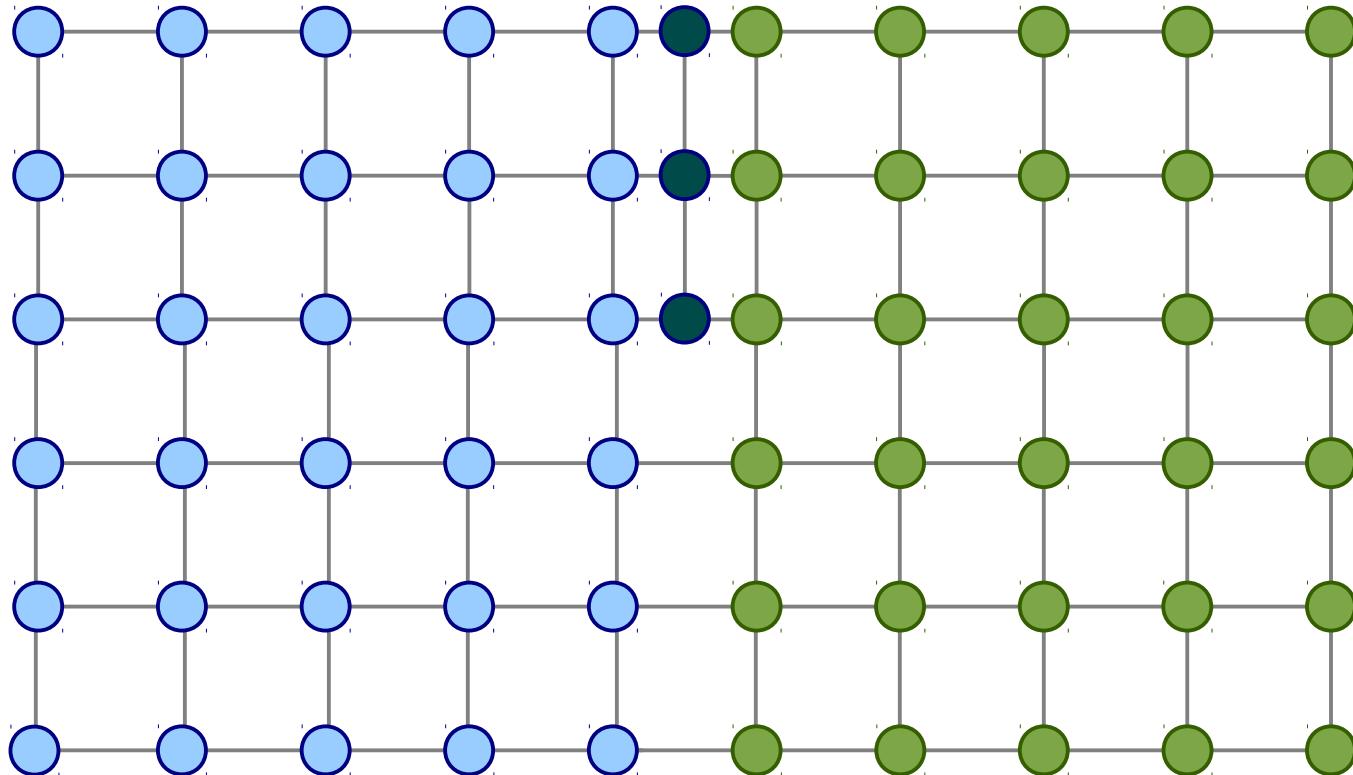
Solution hardening



Precipitate hardening

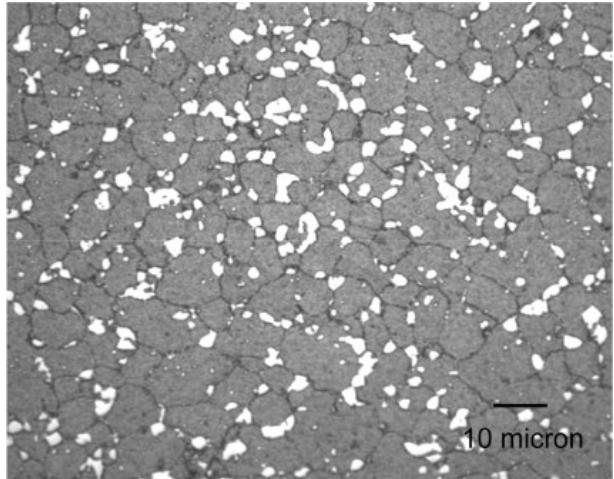


Precipitate hardening

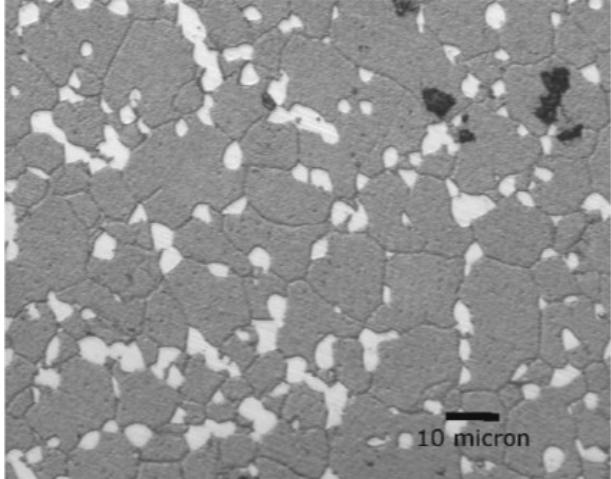


Contemporary alloys

RR1000



N18



Alloy	Firm	Ni	Cr	Co	Mo	Ti	Al	C	Hf	Ta	W	Nb
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Properties

Cost \$lb⁻¹

γ' fraction

Stability

Density gcm⁻³

Yield stress MPa

UTS MPa

Oxidation index

Stress rupture MPa

Resistivity $\mu\Omega\text{cm}$

Entropy Jmol⁻¹K⁻¹

Low cycle fatigue

High cycle fatigue

Weldability

Creep model

Properties

Cost \$lb⁻¹

γ' fraction

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Density gcm⁻³

Yield stress MPa

UTS MPa

Oxidation index

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Resistivity $\mu\Omega\text{cm}$

Entropy Jmol⁻¹K⁻¹

Low cycle fatigue

High cycle fatigue

Weldability

Creep model

$$\begin{aligned}\text{Cost}[\$/\text{lb}] = & 9.59n_{\text{ni}} + 0.94n_{\text{Al}} + 6.77n_{\text{Cr}} \\ & + 16.5n_{\text{Co}} + 19.6n_{\text{Mo}} + 5.44n_{\text{Ti}}\end{aligned}$$

Properties

Collect data for yield stress from 2248 alloys

Cost \$lb⁻¹

γ' fraction

Stability

Density gcm⁻³

Yield stress MPa

UTS MPa

Oxidation index

Stress rupture MPa

Resistivity $\mu\Omega\text{cm}$

Entropy Jmol⁻¹K⁻¹

Low cycle fatigue

High cycle fatigue

Weldability

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γ' fraction

Stability

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Yield stress MPa

UTS MPa

Oxidation index

Stress rupture MPa

Resistivity $\mu\Omega\text{cm}$

Entropy Jmol⁻¹K⁻¹

Low cycle fatigue

High cycle fatigue

Weldability

Creep model

Collect data for yield stress from 2248 alloys



Generate neural network model

$$\text{YS}[\text{MPa}] = F(n_{\text{ni}}, n_{\text{Al}}, n_{\text{Cr}}, n_{\text{Co}}, n_{\text{Mo}}, n_{\text{Ti}}, T_{\text{HT}}, t_{\text{HT}})$$

Properties

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Oxidation index

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Calculate uncertainty in neural network model

Properties

Cost \$lb⁻¹

γ' fraction

Stability

Density gcm⁻³

Yield stress MPa

UTS MPa

Oxidation index

Stress rupture MPa

Resistivity $\mu\Omega\text{cm}$

Entropy Jmol⁻¹K⁻¹

Low cycle fatigue

High cycle fatigue

Weldability

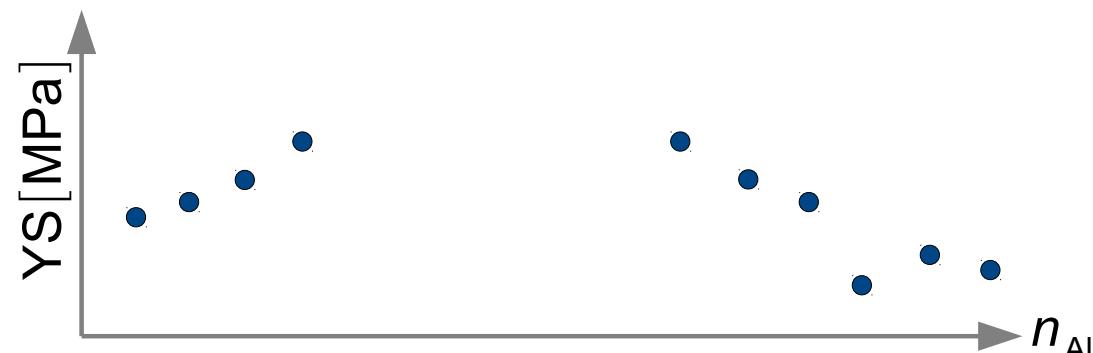
Creep model

Collect data for yield stress from 2248 alloys

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$$\text{YS}[\text{MPa}] = F(n_{\text{ni}}, n_{\text{Al}}, n_{\text{Cr}}, n_{\text{Co}}, n_{\text{Mo}}, n_{\text{Ti}}, T_{\text{HT}}, t_{\text{HT}})$$

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High cycle fatigue

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Creep model

Collect data for yield stress from 2248 alloys

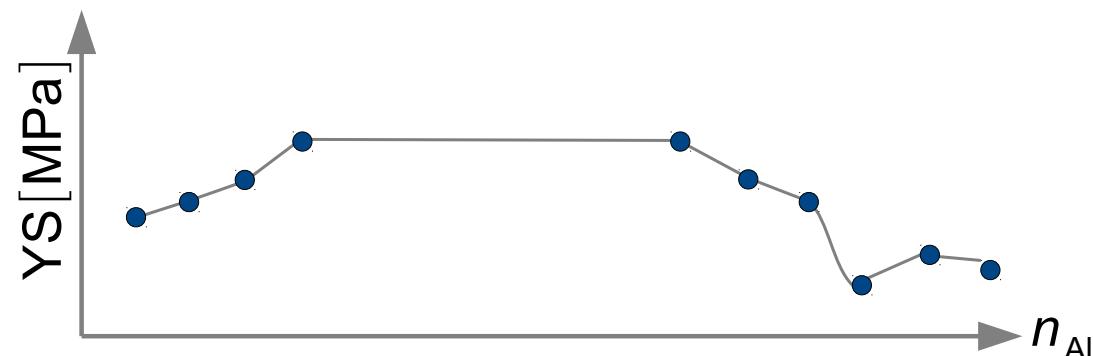


Generate neural network model

$$\text{YS}[\text{MPa}] = F(n_{\text{ni}}, n_{\text{Al}}, n_{\text{Cr}}, n_{\text{Co}}, n_{\text{Mo}}, n_{\text{Ti}}, T_{\text{HT}}, t_{\text{HT}})$$



Calculate uncertainty in neural network model



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Collect data for yield stress from 2248 alloys

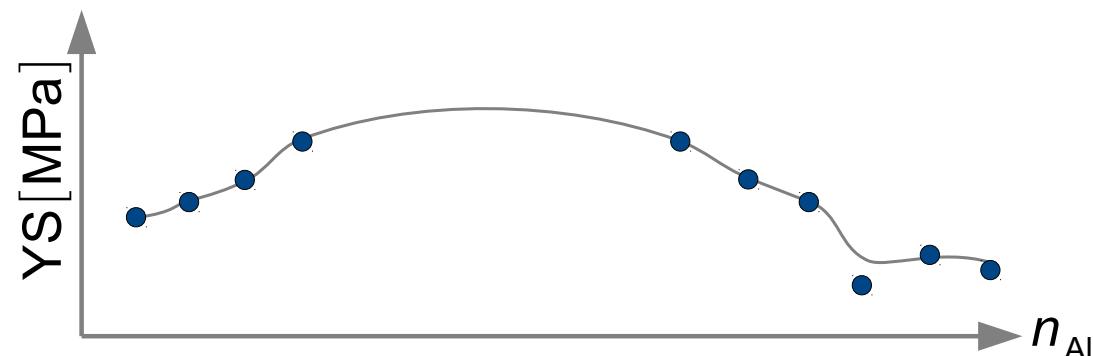


Generate neural network model

$$\text{YS}[\text{MPa}] = F(n_{\text{ni}}, n_{\text{Al}}, n_{\text{Cr}}, n_{\text{Co}}, n_{\text{Mo}}, n_{\text{Ti}}, T_{\text{HT}}, t_{\text{HT}})$$



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Collect data for yield stress from 2248 alloys

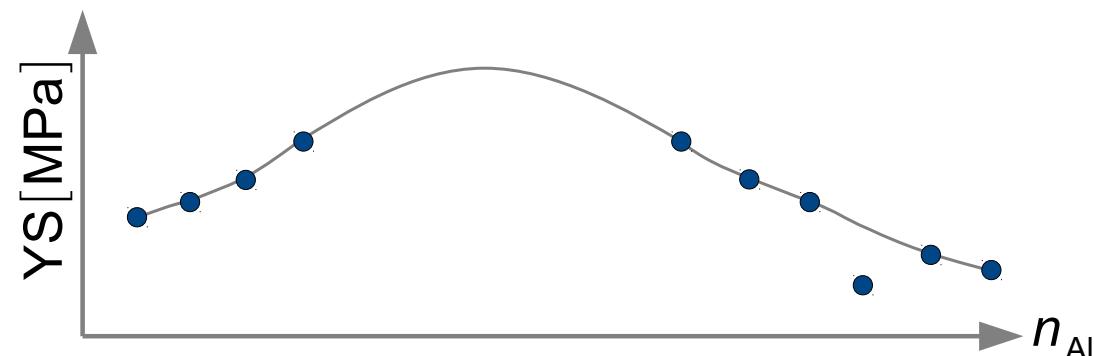


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$$\text{YS}[\text{MPa}] = F(n_{\text{ni}}, n_{\text{Al}}, n_{\text{Cr}}, n_{\text{Co}}, n_{\text{Mo}}, n_{\text{Ti}}, T_{\text{HT}}, t_{\text{HT}})$$



Calculate uncertainty in neural network model



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γ' fraction

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Oxidation index

Stress rupture MPa

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Entropy Jmol⁻¹K⁻¹

Low cycle fatigue

High cycle fatigue

Weldability

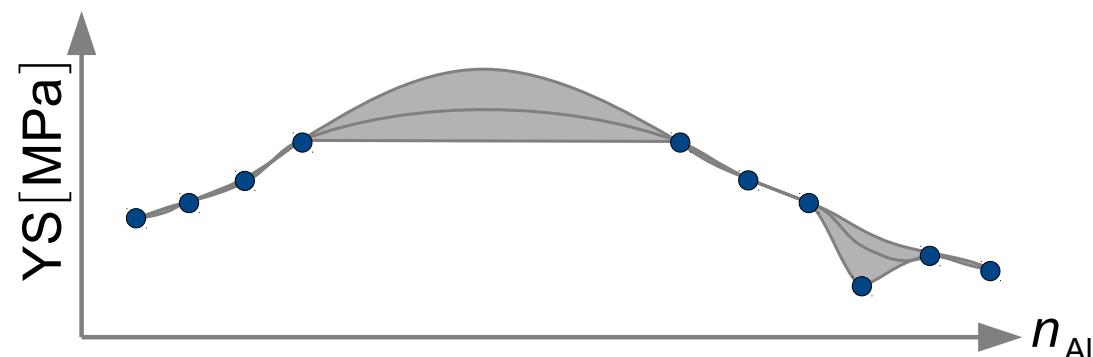
Creep model

Collect data for yield stress from 2248 alloys

Generate neural network model

$$\text{YS}[\text{MPa}] = F(n_{\text{ni}}, n_{\text{Al}}, n_{\text{Cr}}, n_{\text{Co}}, n_{\text{Mo}}, n_{\text{Ti}}, T_{\text{HT}}, t_{\text{HT}})$$

Calculate uncertainty in neural network model



Properties

Cost \$lb⁻¹

γ' fraction

Stability

Density gcm⁻³

Yield stress MPa

UTS MPa

Oxidation index

Stress rupture MPa

Resistivity $\mu\Omega\text{cm}$

Entropy Jmol⁻¹K⁻¹

Low cycle fatigue

High cycle fatigue

Weldability

Creep model

Calculate grid of

$$F_{(\gamma, \gamma')}(n_{\text{ni}}, n_{\text{Al}}, n_{\text{Cr}}, n_{\text{Co}}, n_{\text{Mo}}, n_{\text{Ti}})$$

Properties

Cost \$lb⁻¹

γ' fraction

Stability

Density gcm⁻³

Yield stress MPa

UTS MPa

Oxidation index

Stress rupture MPa

Resistivity $\mu\Omega\text{cm}$

Entropy Jmol⁻¹K⁻¹

Low cycle fatigue

High cycle fatigue

Weldability

Creep model

Calculate grid of

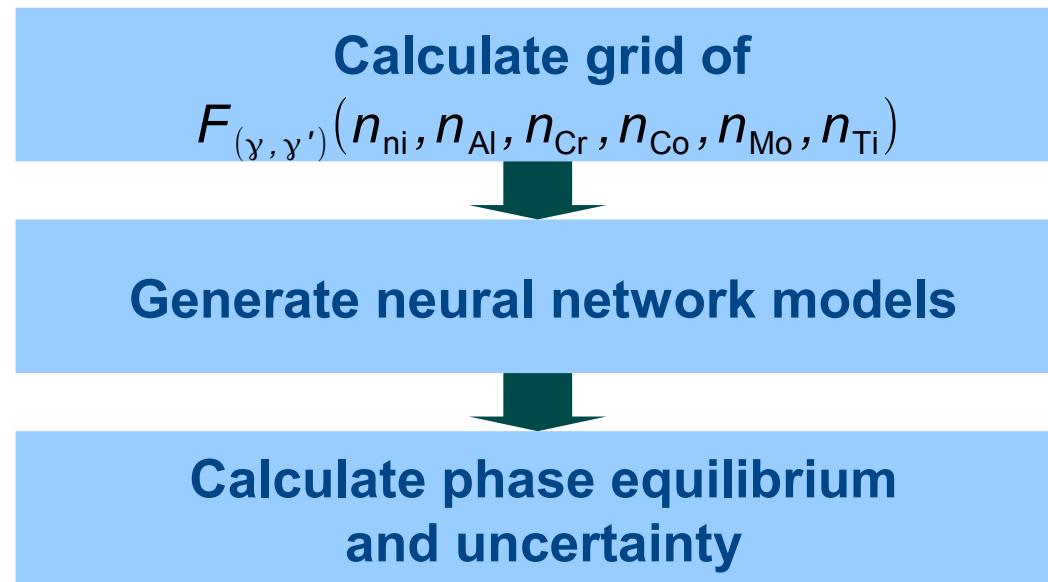
$$F_{(\gamma, \gamma')}(n_{\text{ni}}, n_{\text{Al}}, n_{\text{Cr}}, n_{\text{Co}}, n_{\text{Mo}}, n_{\text{Ti}})$$



Generate neural network models

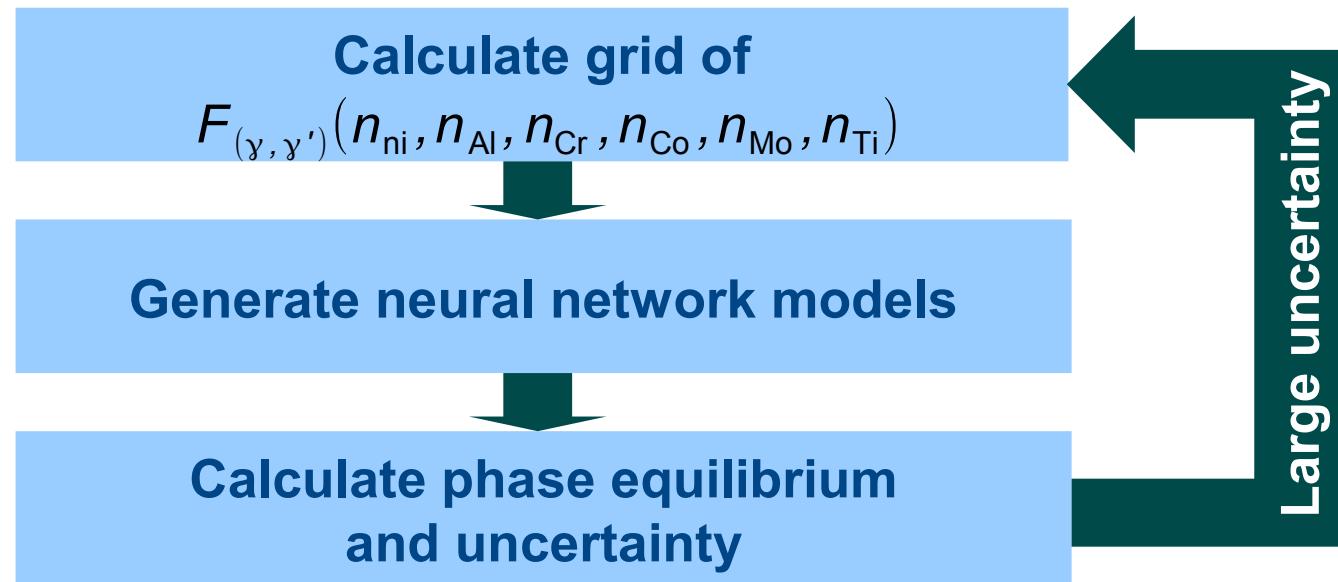
Properties

Cost \$lb⁻¹
 γ' fraction
Stability
Density gcm⁻³
Yield stress MPa
UTS MPa
Oxidation index
Stress rupture MPa
Resistivity $\mu\Omega\text{cm}$
Entropy Jmol⁻¹K⁻¹
Low cycle fatigue
High cycle fatigue
Weldability
Creep model



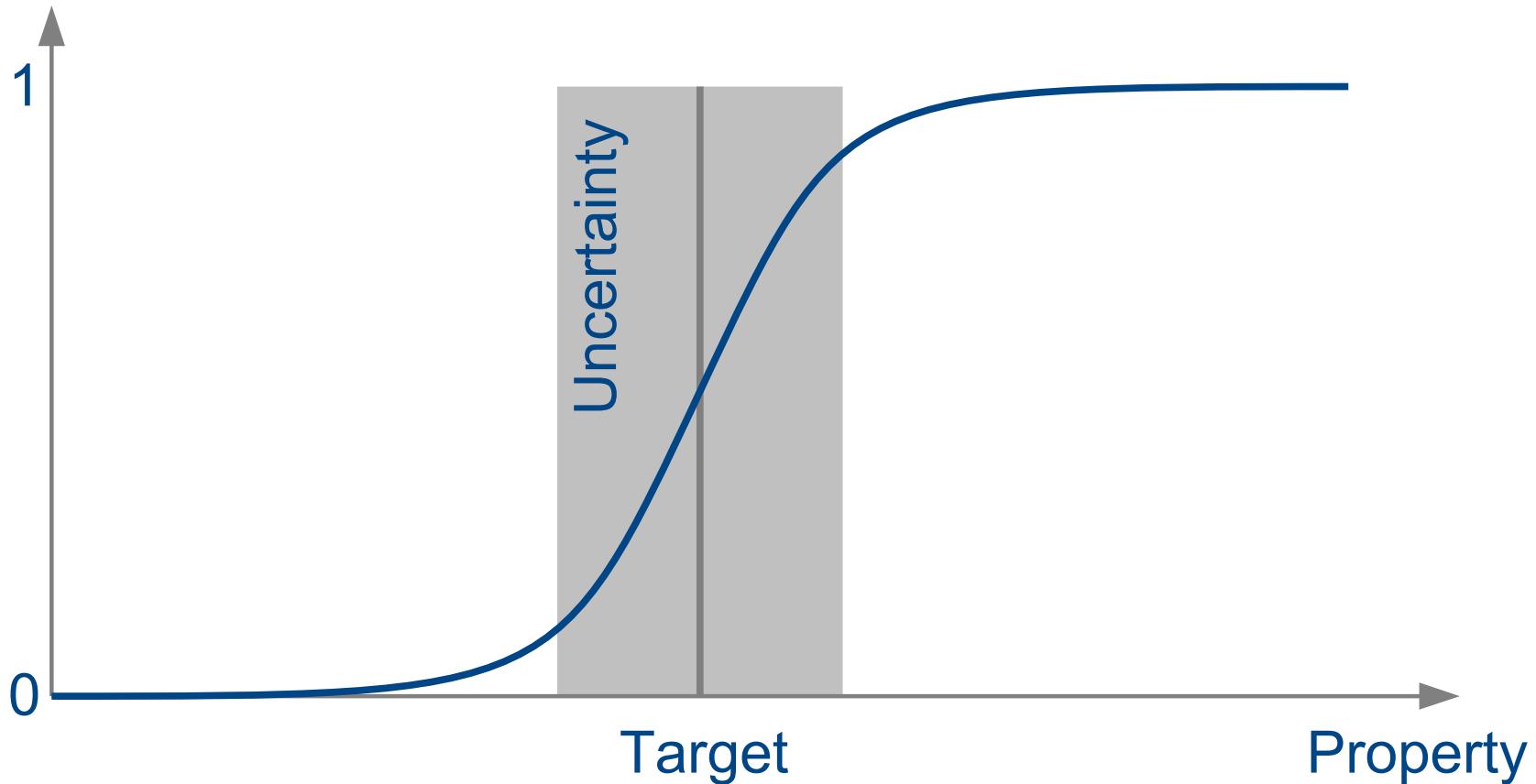
Properties

Cost \$lb⁻¹
 γ' fraction
Stability
Density gcm⁻³
Yield stress MPa
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Oxidation index
Stress rupture MPa
Resistivity $\mu\Omega\text{cm}$
Entropy Jmol⁻¹K⁻¹
Low cycle fatigue
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Creep model



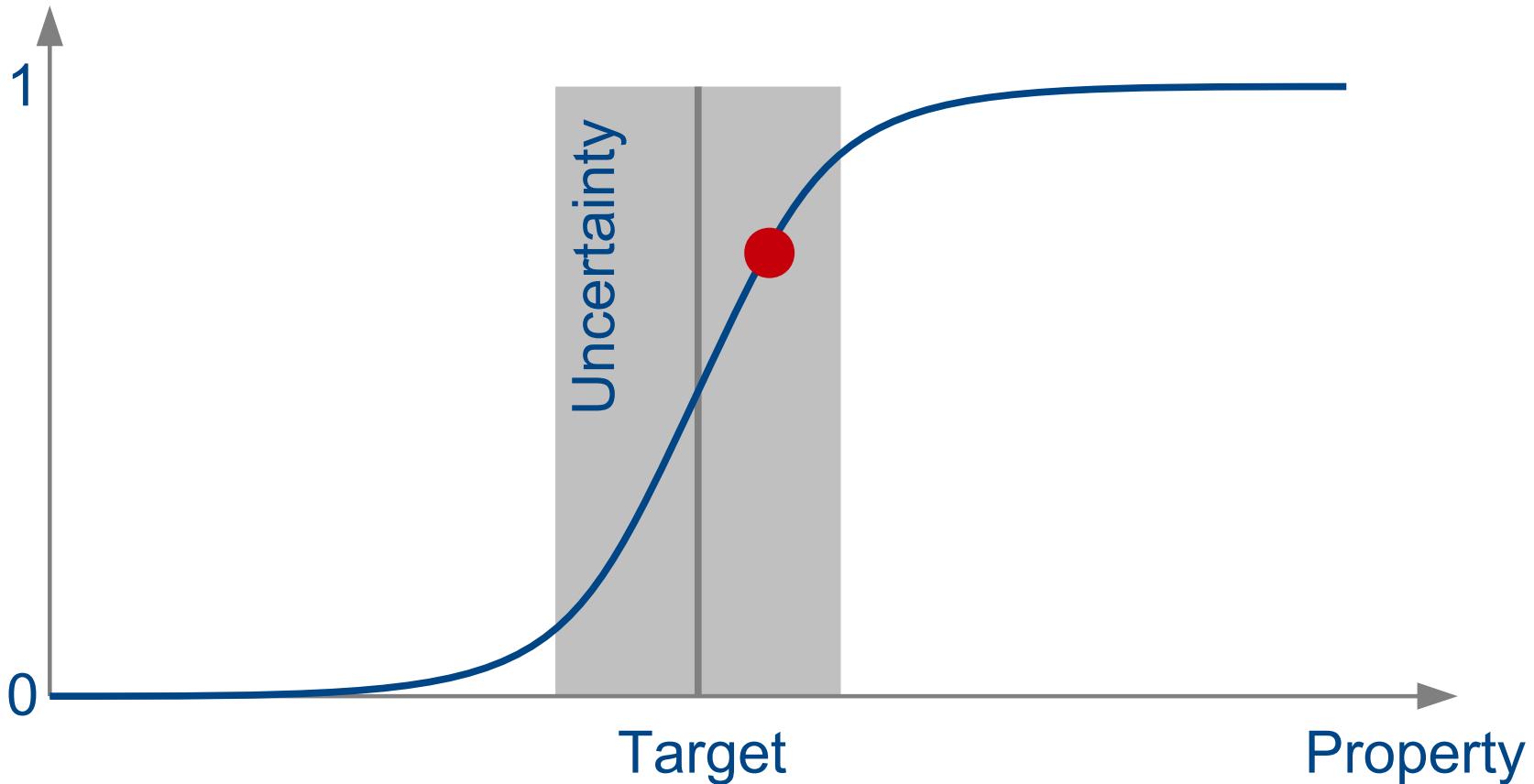
Probability

Probability



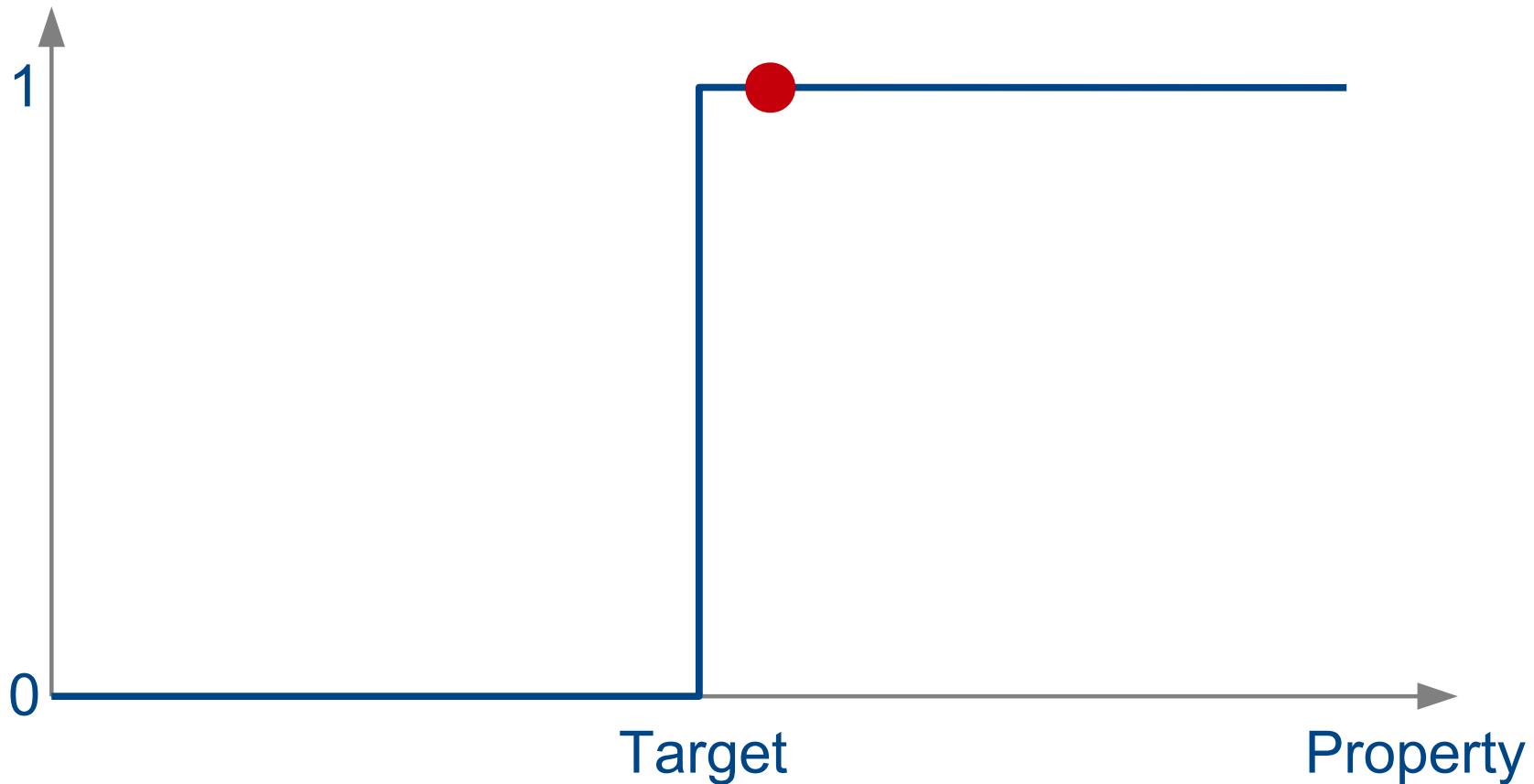
Probability

Probability



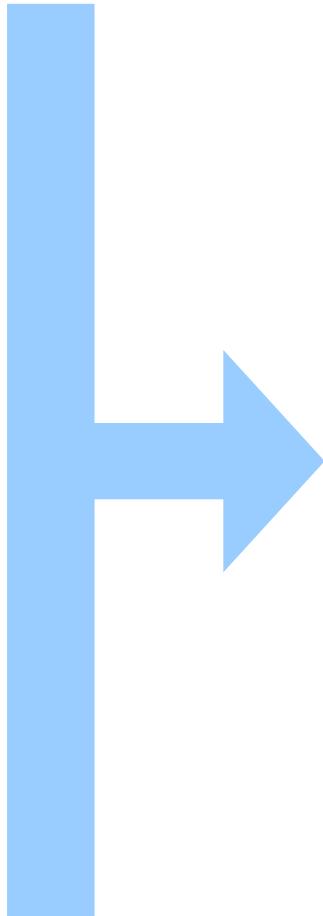
Probability

Probability



Probability

Cost \$lb ⁻¹	$P_{\text{cost}}(\mathbf{C})$
γ' fraction	$P_{\gamma'}(\mathbf{C})$
Stability	$P_{\text{stable}}(\mathbf{C})$
Density gcm ⁻³	$P_{\text{density}}(\mathbf{C})$
Yield stress MPa	$P_{\text{ys}}(\mathbf{C})$
UTS MPa	$P_{\text{UTS}}(\mathbf{C})$
Oxidation index	$P_{\text{oxidize}}(\mathbf{C})$
Stress rupture MPa	$P_{\text{SR}}(\mathbf{C})$
Resistivity $\mu\Omega\text{cm}$	$P_{\text{resis}}(\mathbf{C})$
Entropy $\text{Jmol}^{-1}\text{K}^{-1}$	$P_{\text{entropy}}(\mathbf{C})$
Low cycle fatigue	$P_{\text{LCF}}(\mathbf{C})$
High cycle fatigue	$P_{\text{HCF}}(\mathbf{C})$
Weldability	$P_{\text{weld}}(\mathbf{C})$
Creep model	$P_{\text{creep}}(\mathbf{C})$



$$P_{\text{spec}}(\mathbf{C})$$

Optimization – probability

10 specified properties,
each with probability of 0.5

$0.5^{10} = 0.001$ chance of success

Multidimensional design space

Cr



Co



Mo



W



Ta



Nb



Al



Ti



Fe



Mn



Si



C



B



Zr



Cu



N



P



V



Hf



Mg



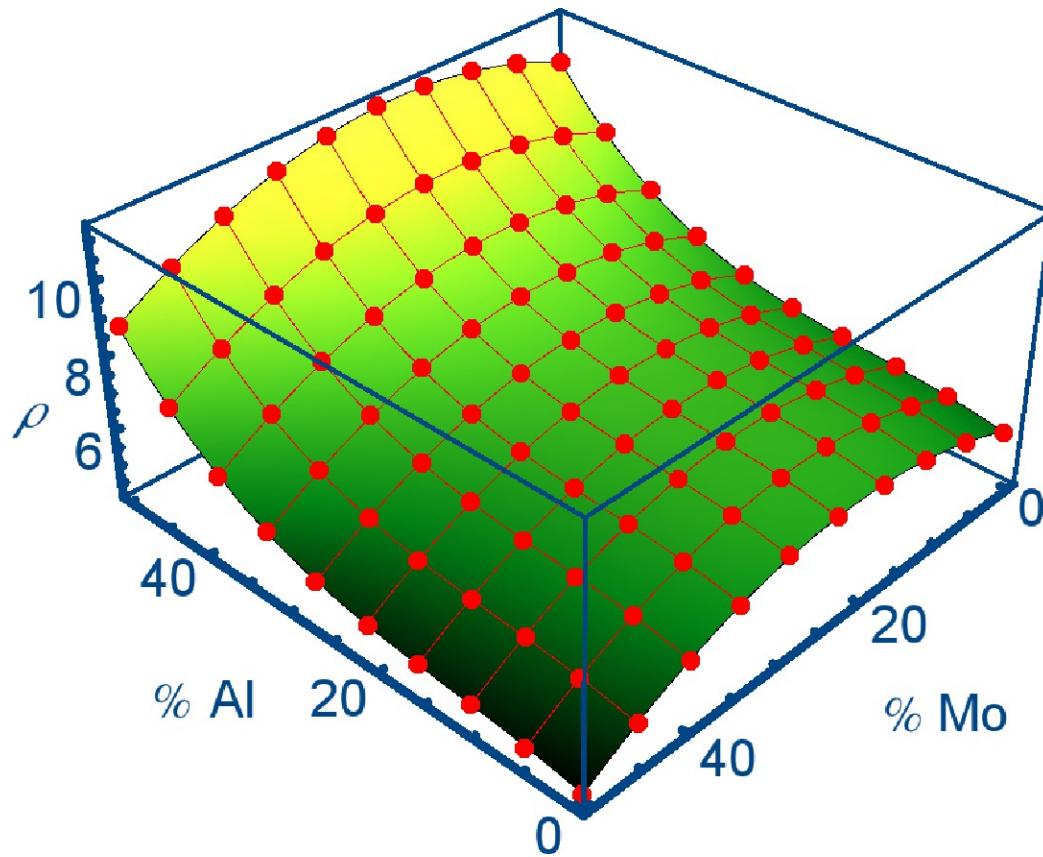
Ni



Heat
treatment

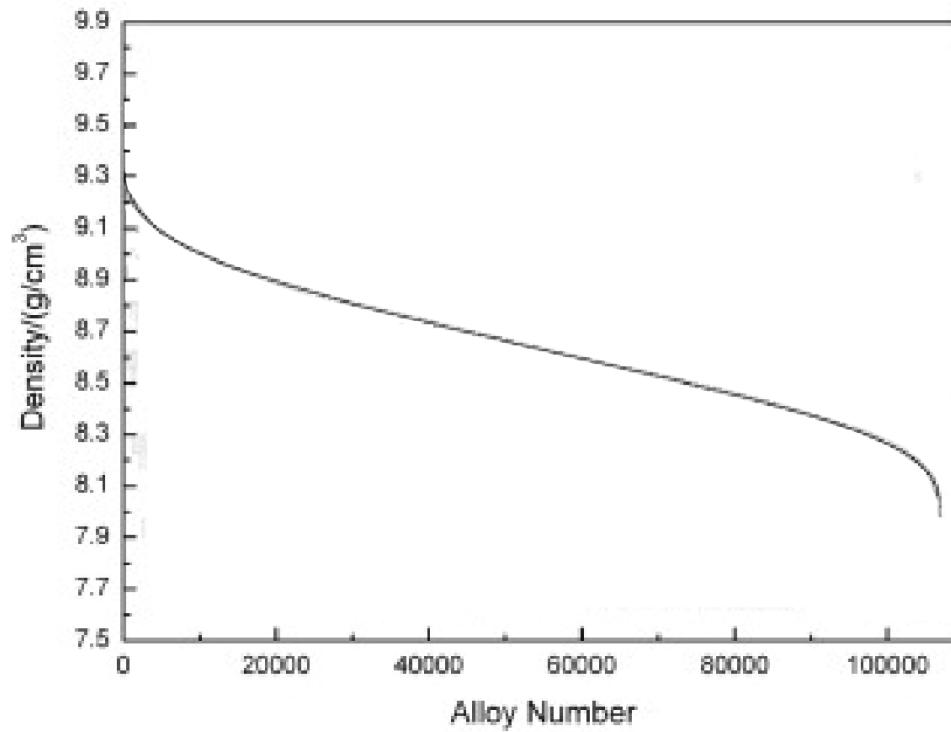


Optimization – tradeoff diagrams



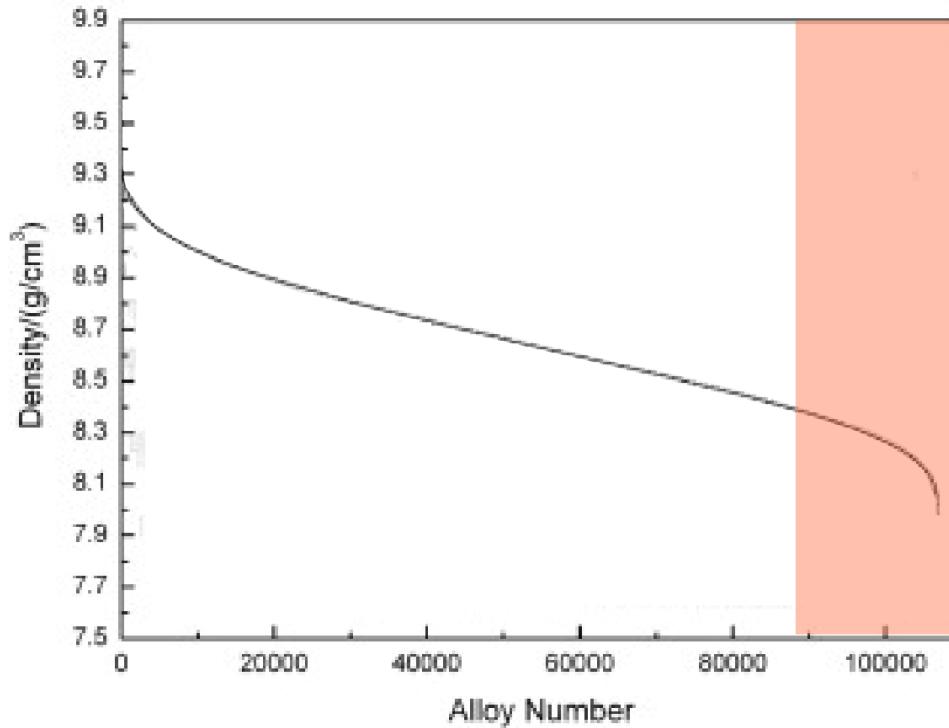
R.C. Reed, T. Tao & N. Warnken, Acta Materialia 57, 5898 (2009)

Optimization – tradeoff diagrams



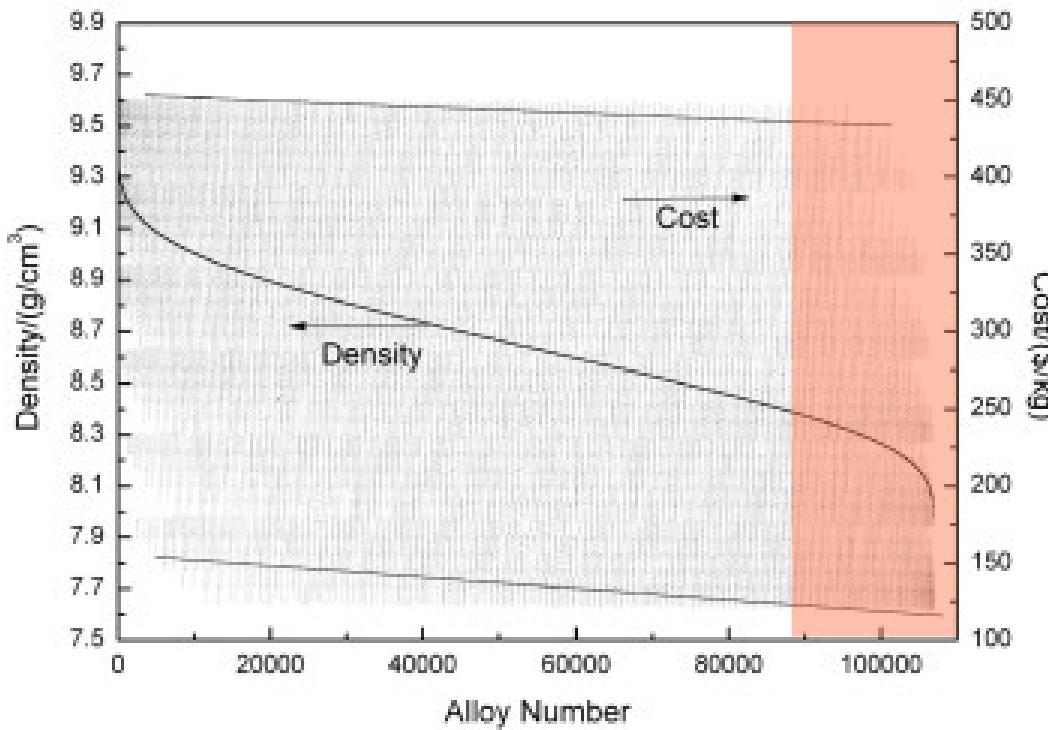
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Optimization – tradeoff diagrams



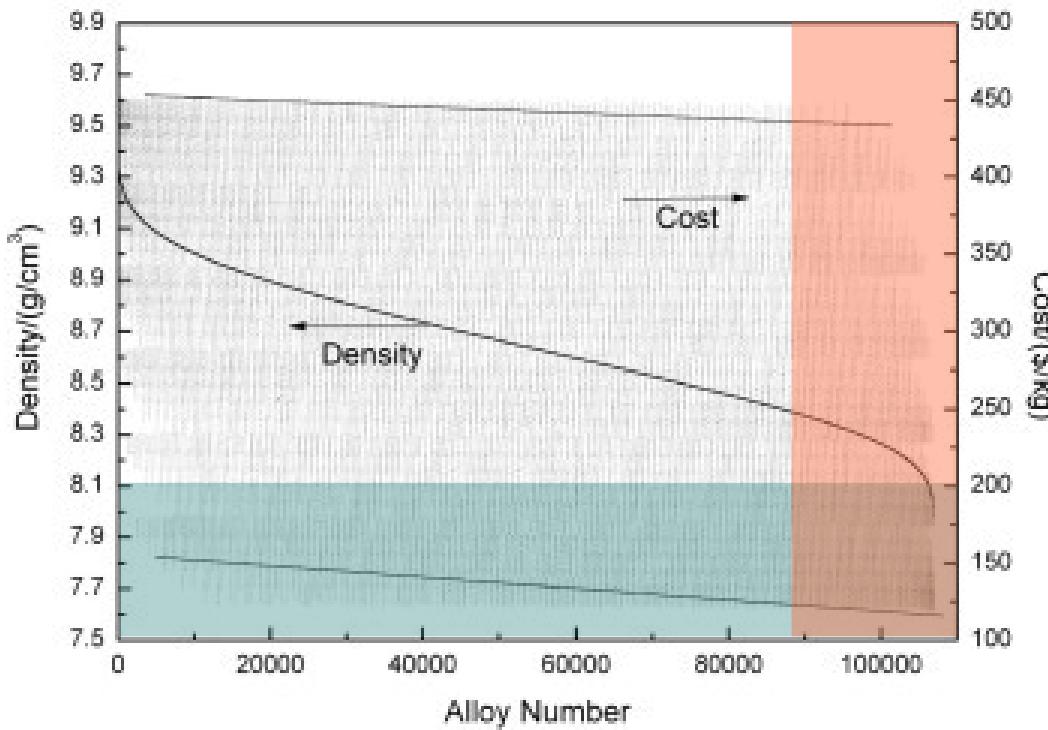
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Optimization – tradeoff diagrams



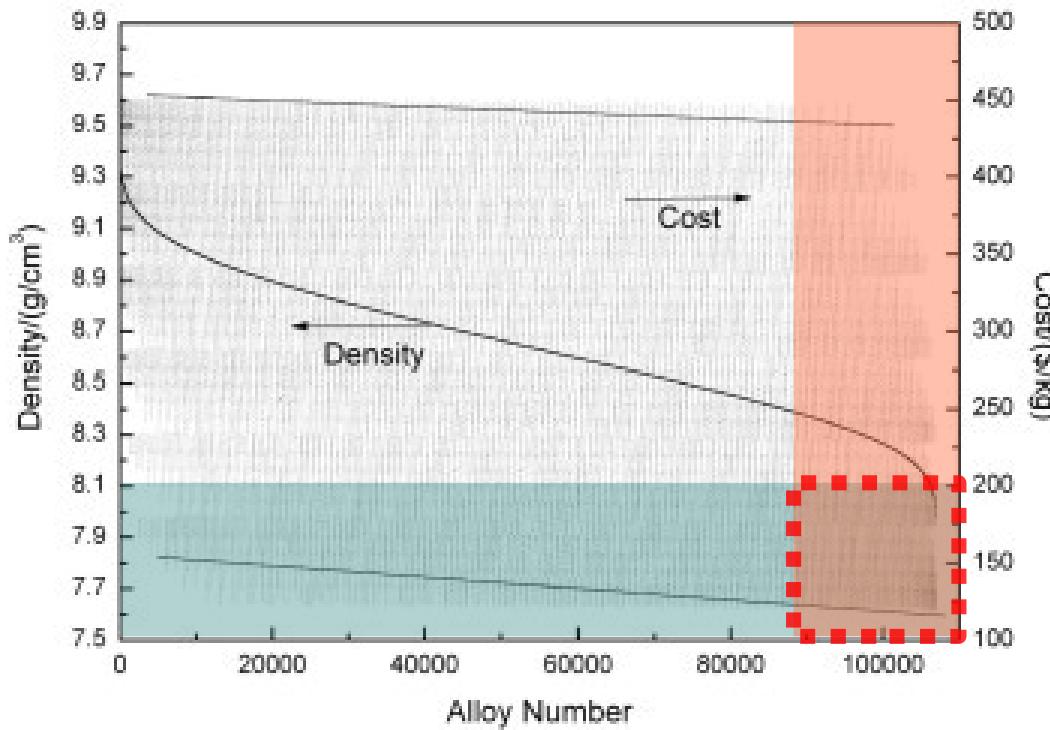
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Optimization – tradeoff diagrams



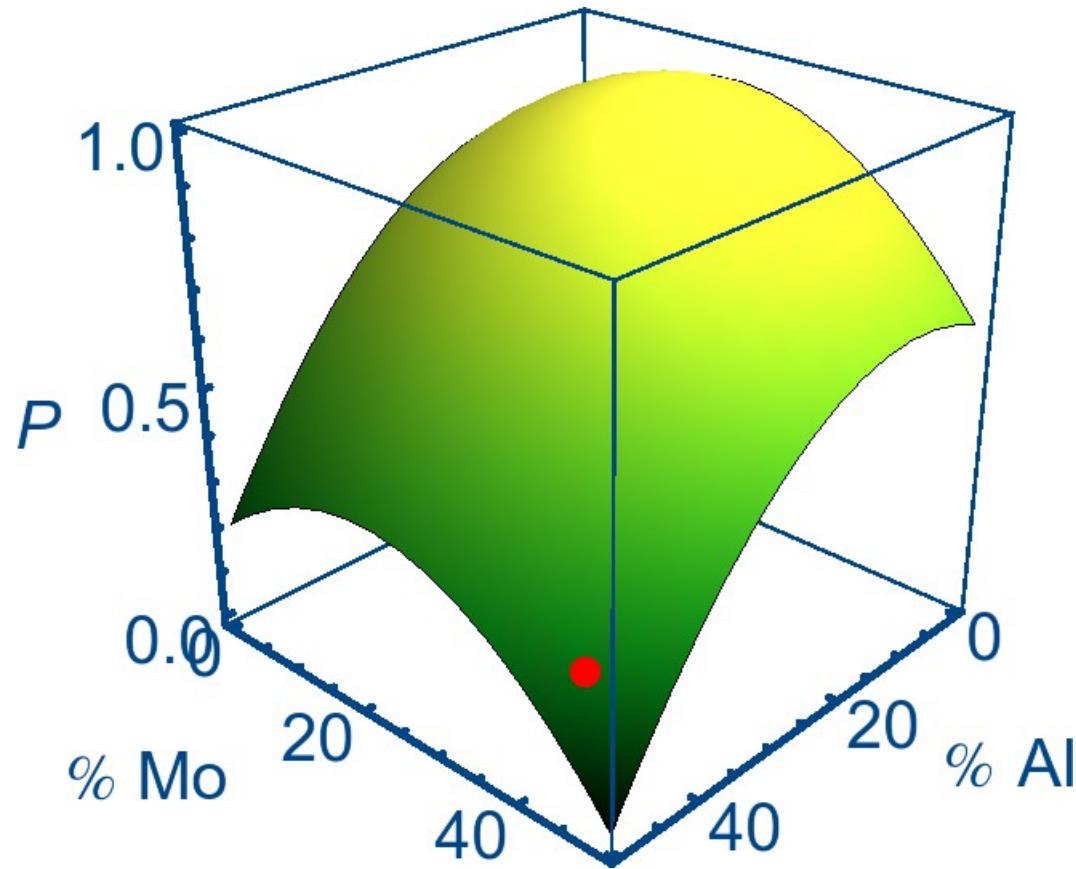
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Optimization – tradeoff diagrams

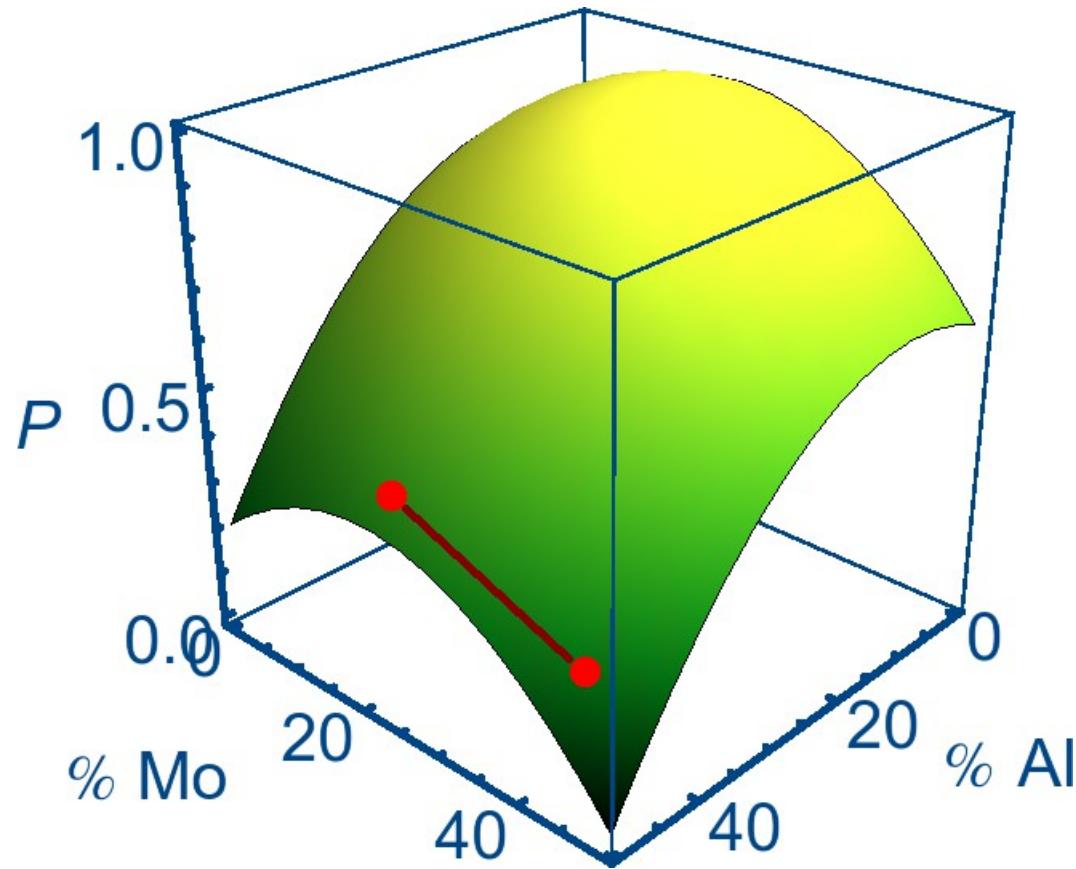
30 design variables, at 0.1% accuracy,
and evaluation time of 1ms

$$1000^{30} = 3 \times 10^{79} \text{ years}$$

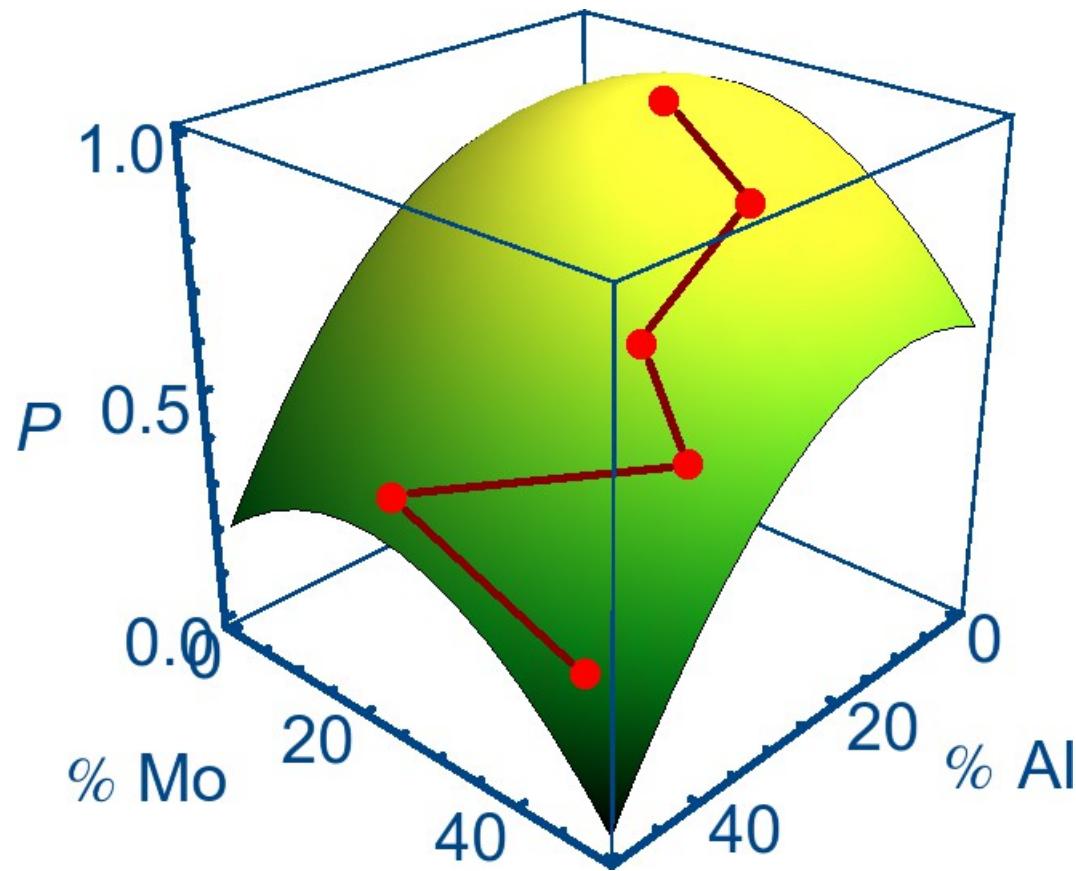
Optimization – replica exchange sampling



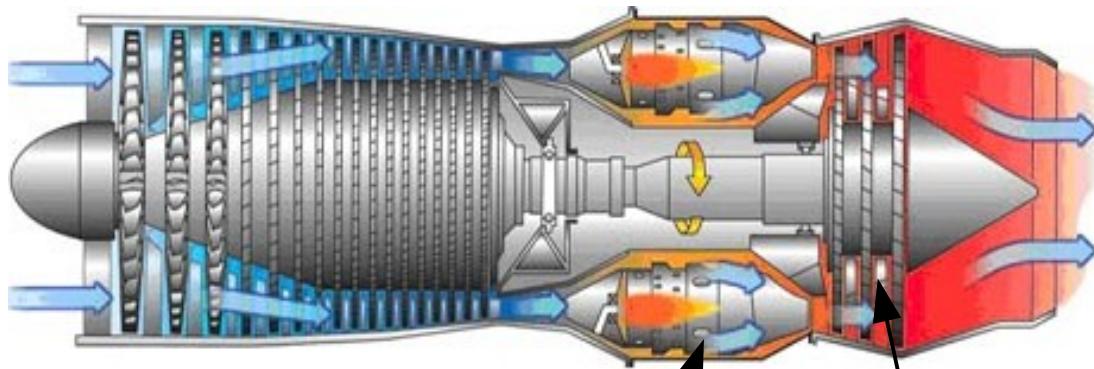
Optimization – replica exchange sampling



Optimization – replica exchange sampling



Predicted alloys



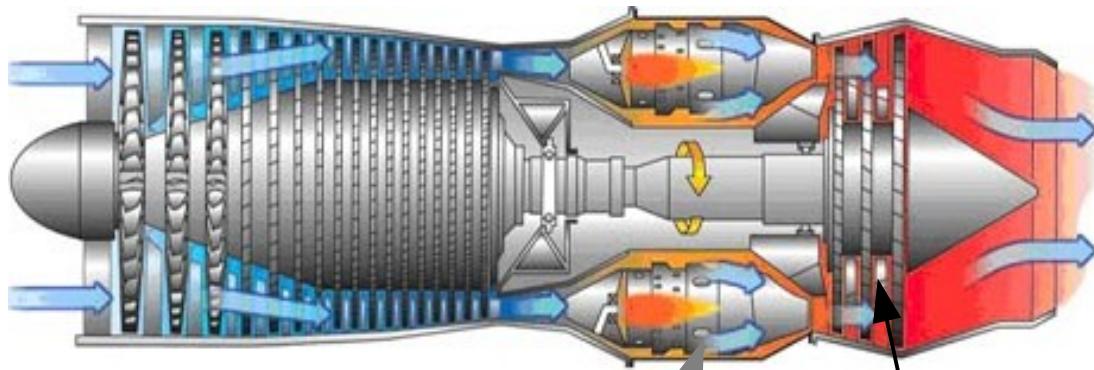
Combustor
liner

2x disc
alloy



2x forging
hammer

Predicted alloys



Combustor
liner

**2x disc
alloy**



2x forging
hammer

Case study: improved disc alloy

										
Ni	Cr	Co	Mo	Ti	Al	Ta	Hf	C	T	t
52	15	19	5	3.6	3	2	0.5	0.1	800	8

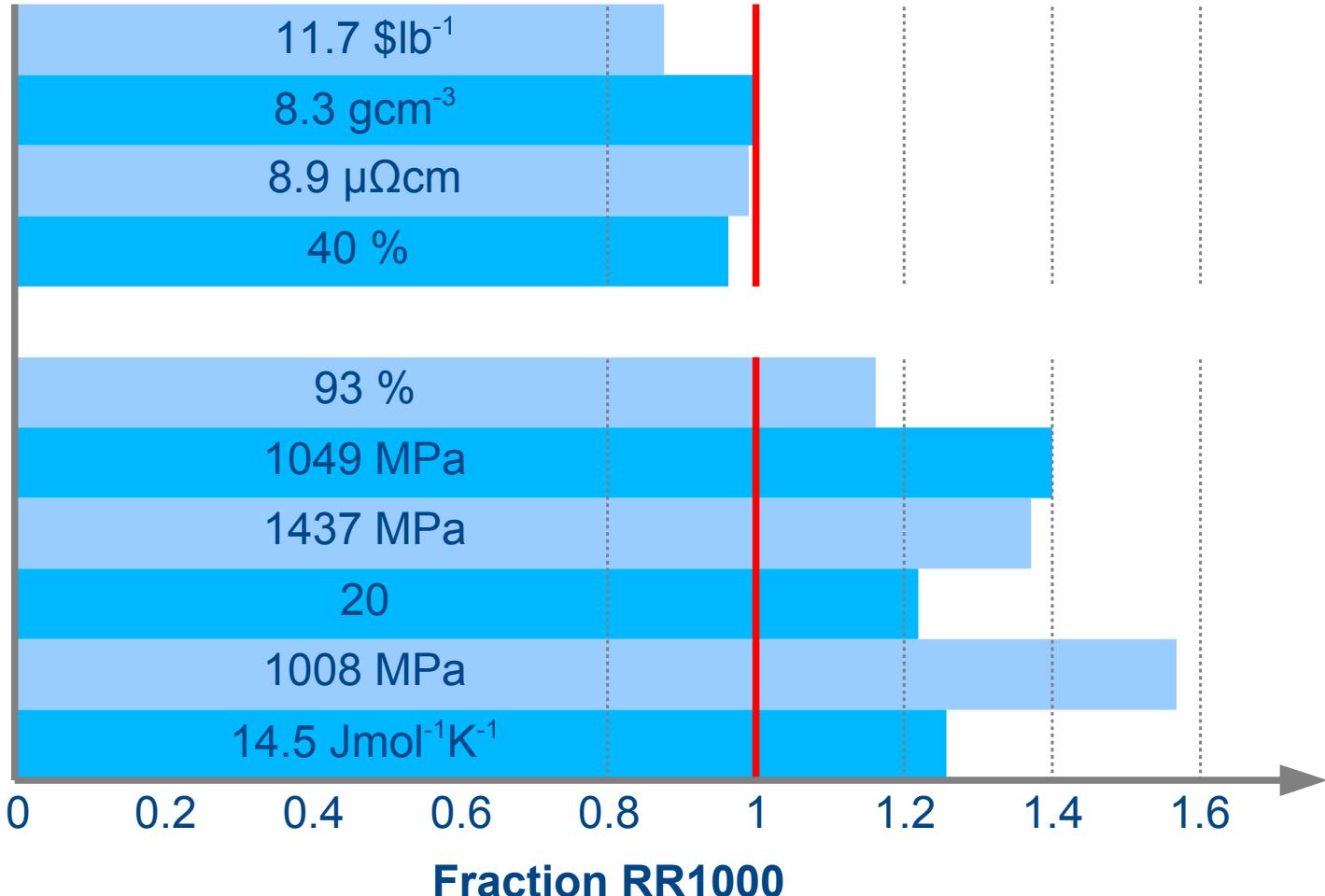
Case study: improved disc alloy

										
Ni	Cr	Co	Mo	Ti	Al	Ta	Hf	C	T	t
56	17	1.0	4.0	1.5	4.3	0.2	0.1	0.2	980	61

							
W	Mn	B	V	Si	Zr	Nb	Fe
6.0	0.1	0.1	0.1	0.1	0.2	5.6	3.4

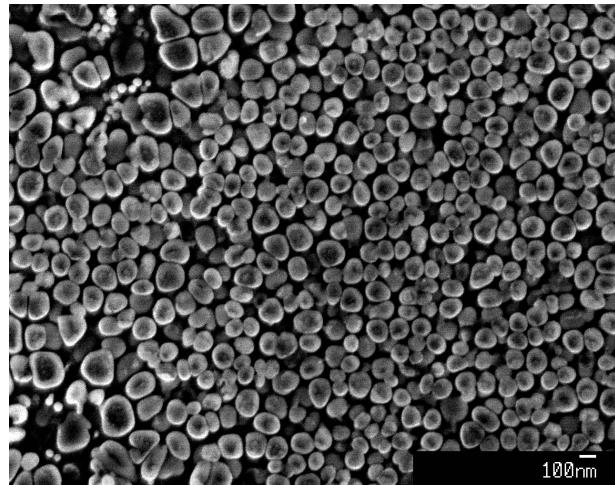
Case study: improved disc alloy

Cost
Density
Resistivity
 γ' fraction



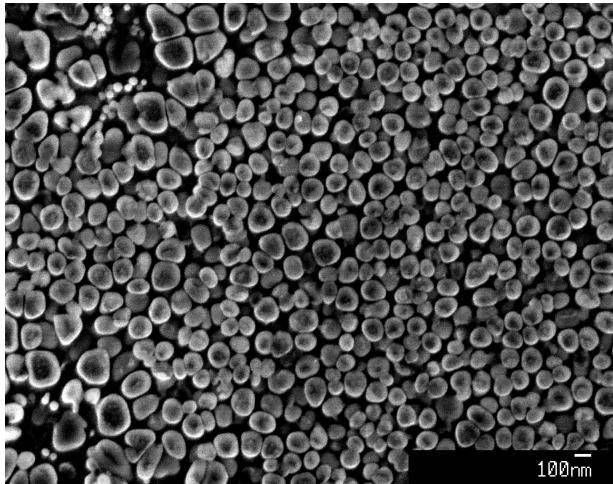
Electron micrograph – Ni disc alloy

Ni disc alloy

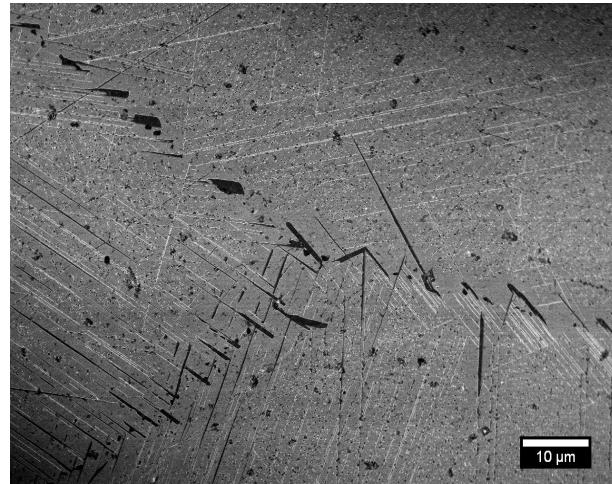


Electron micrograph – Ni disc alloy

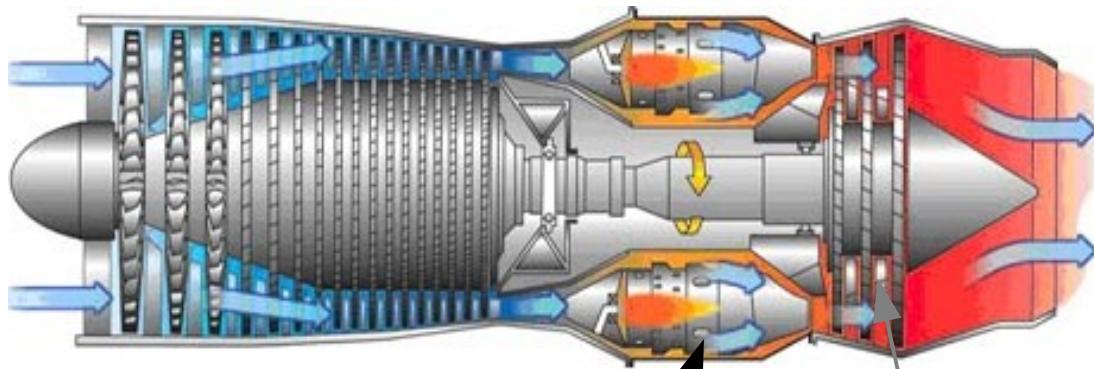
Ni disc alloy



η contaminated alloy



Predicted alloys



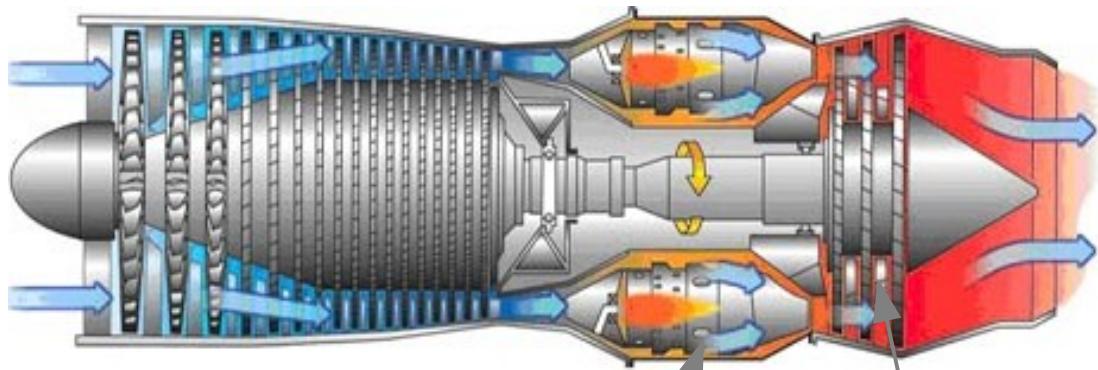
Combustor
liner

2x disc
alloy



2x forging
hammer

Predicted alloys



Combustor
liner

2x disc
alloy



**2x forging
hammer**

Case study: improved forging alloy



Mo



Ti



C



Zr

TZM

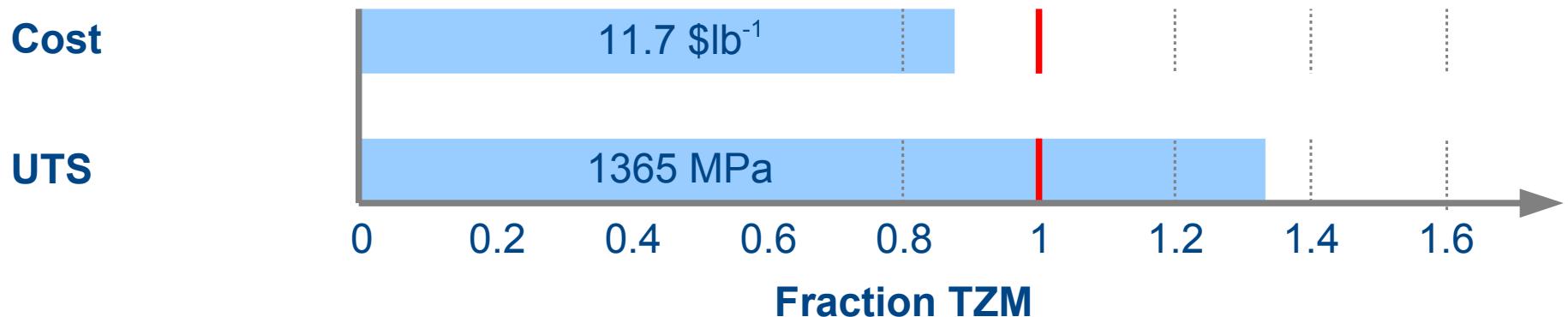
99.4

0.5

0.02

0.08

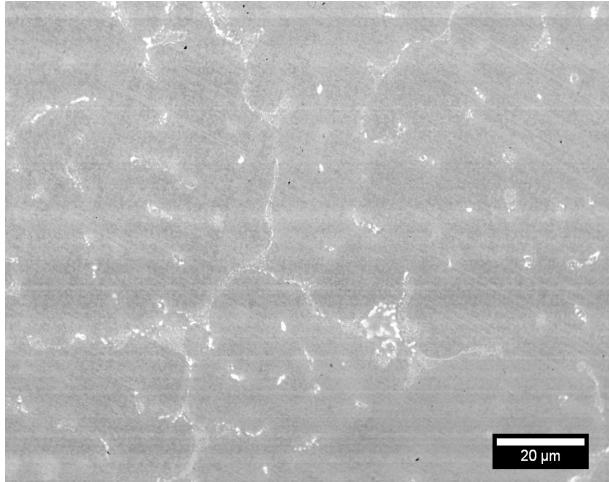
Case study: improved forging alloy



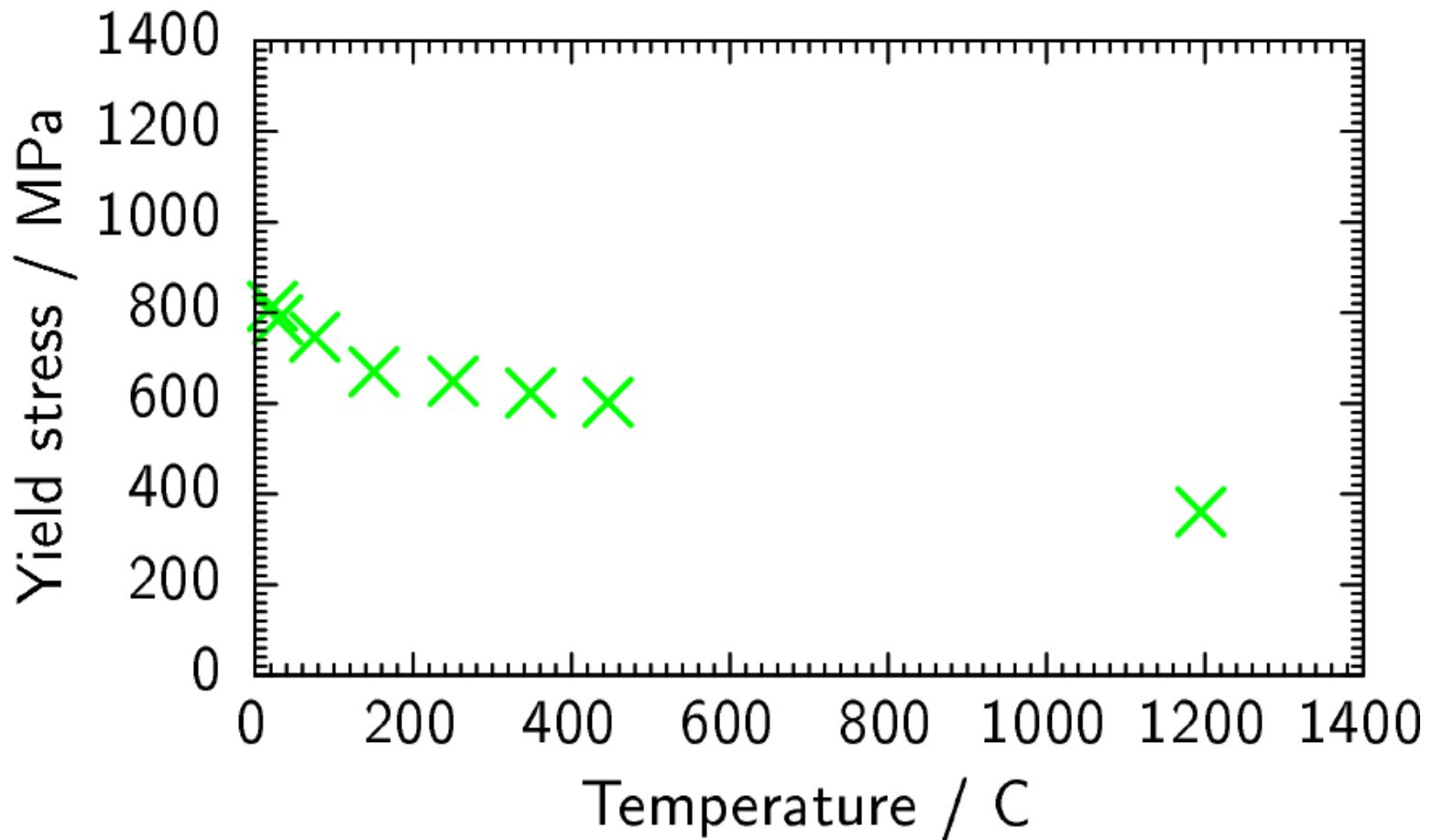
	Mo	Ti	C	Zr	Hf	W	Nb
TZM	99.4	0.5	0.02	0.08			
Optimal	82.7	1.0	0.2	0.9	9.0	0.5	5.7

Electron micrograph – Mo forging alloy

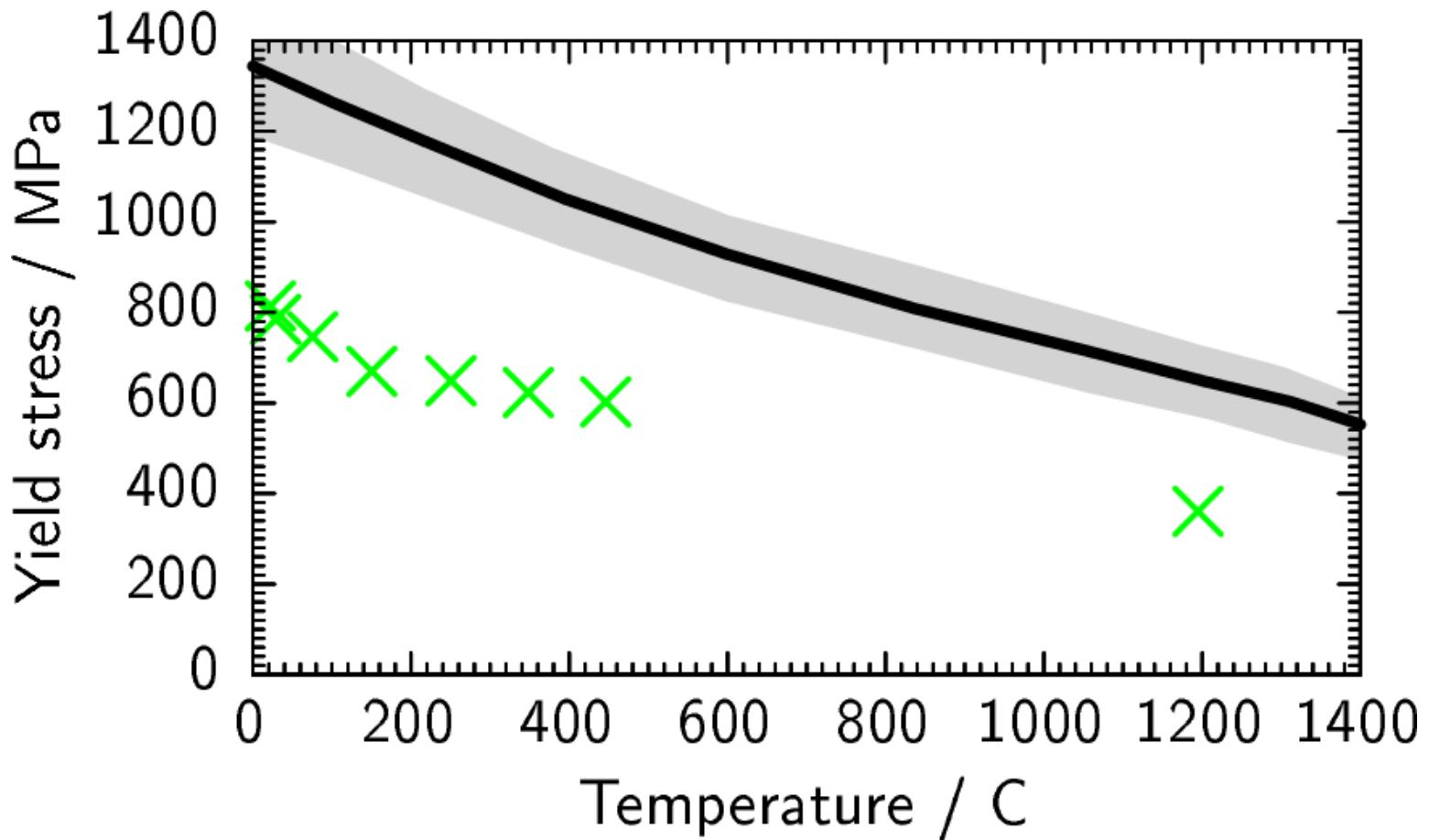
Mo forging alloy



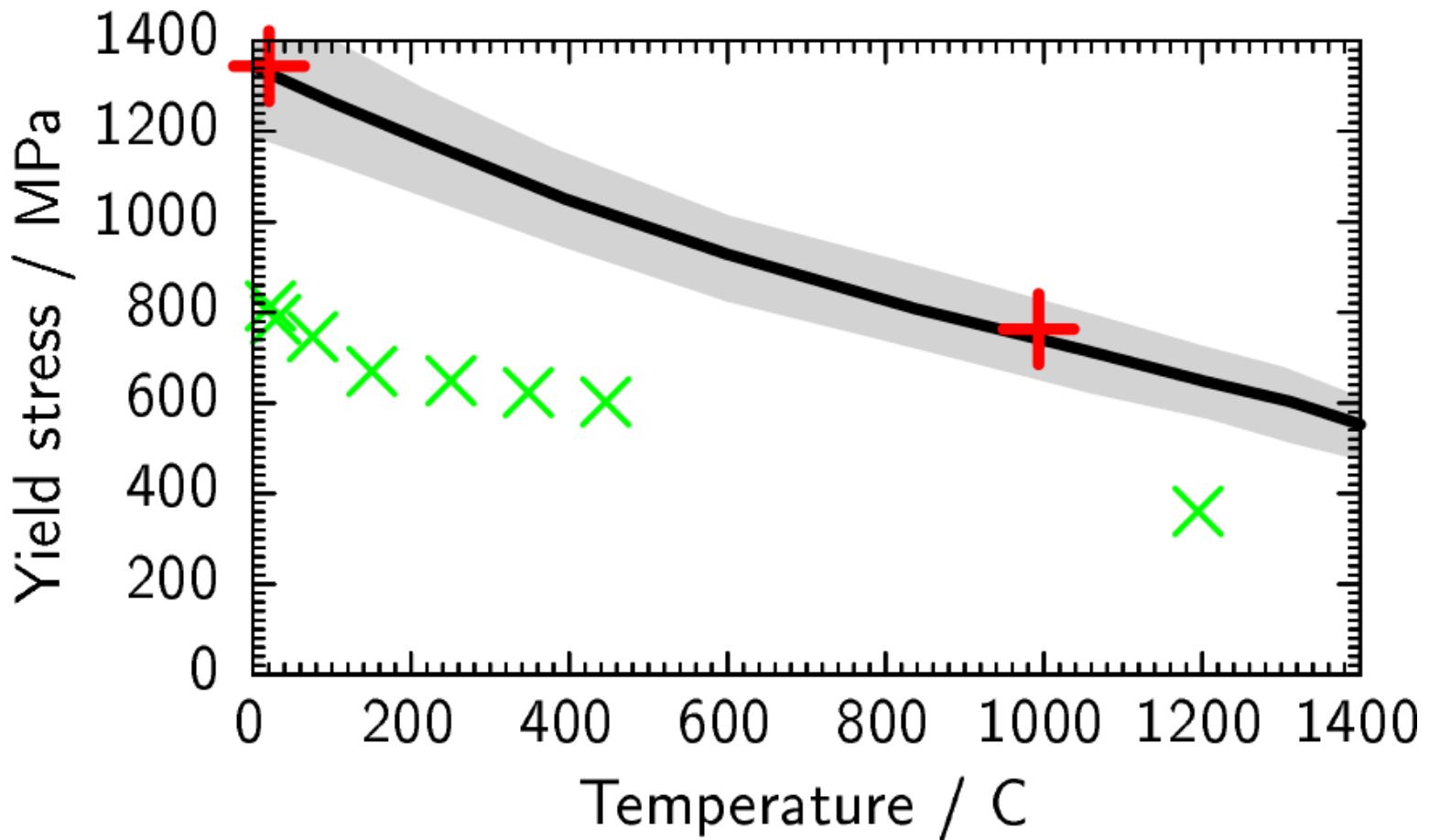
Yield stress



Yield stress



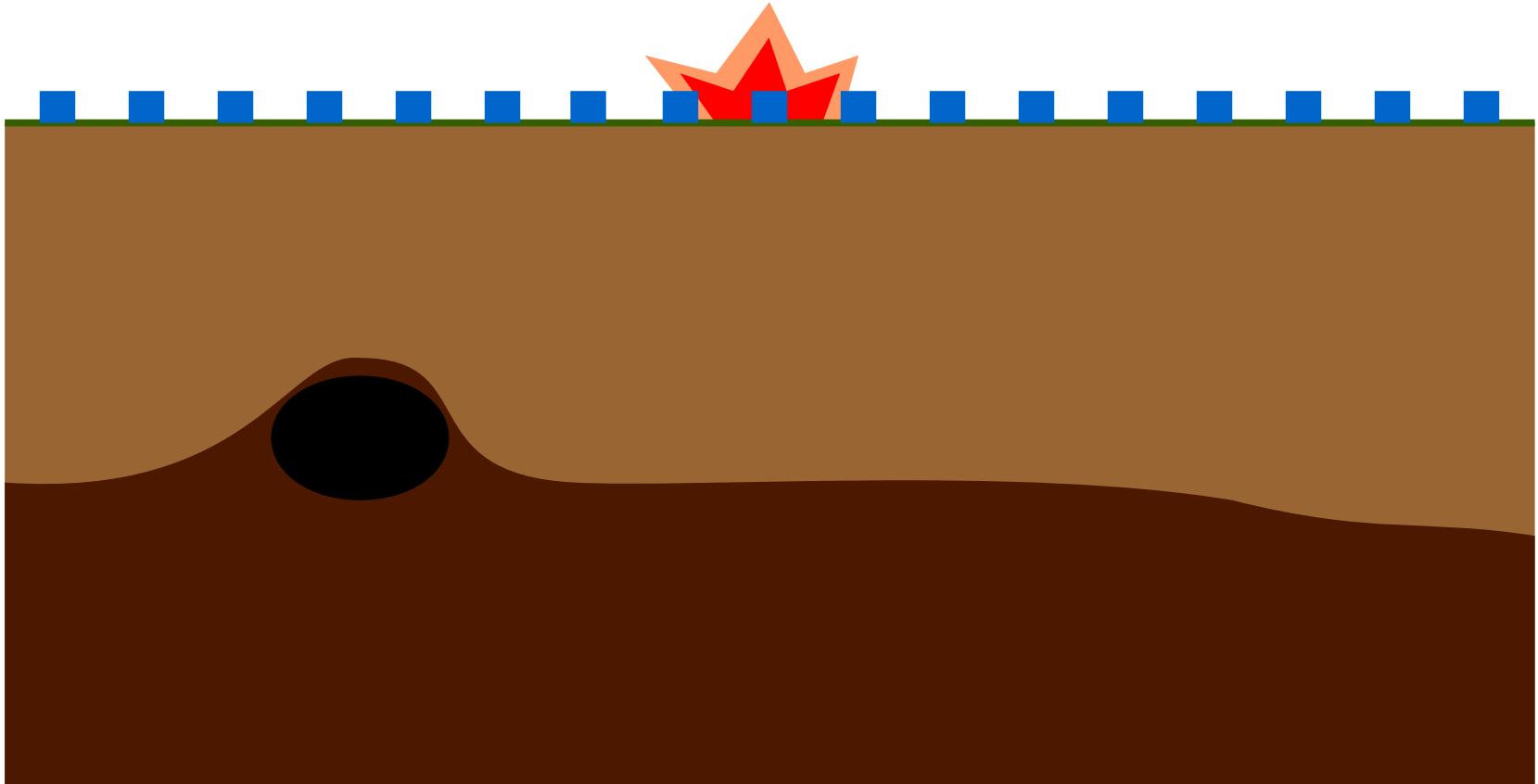
Yield stress



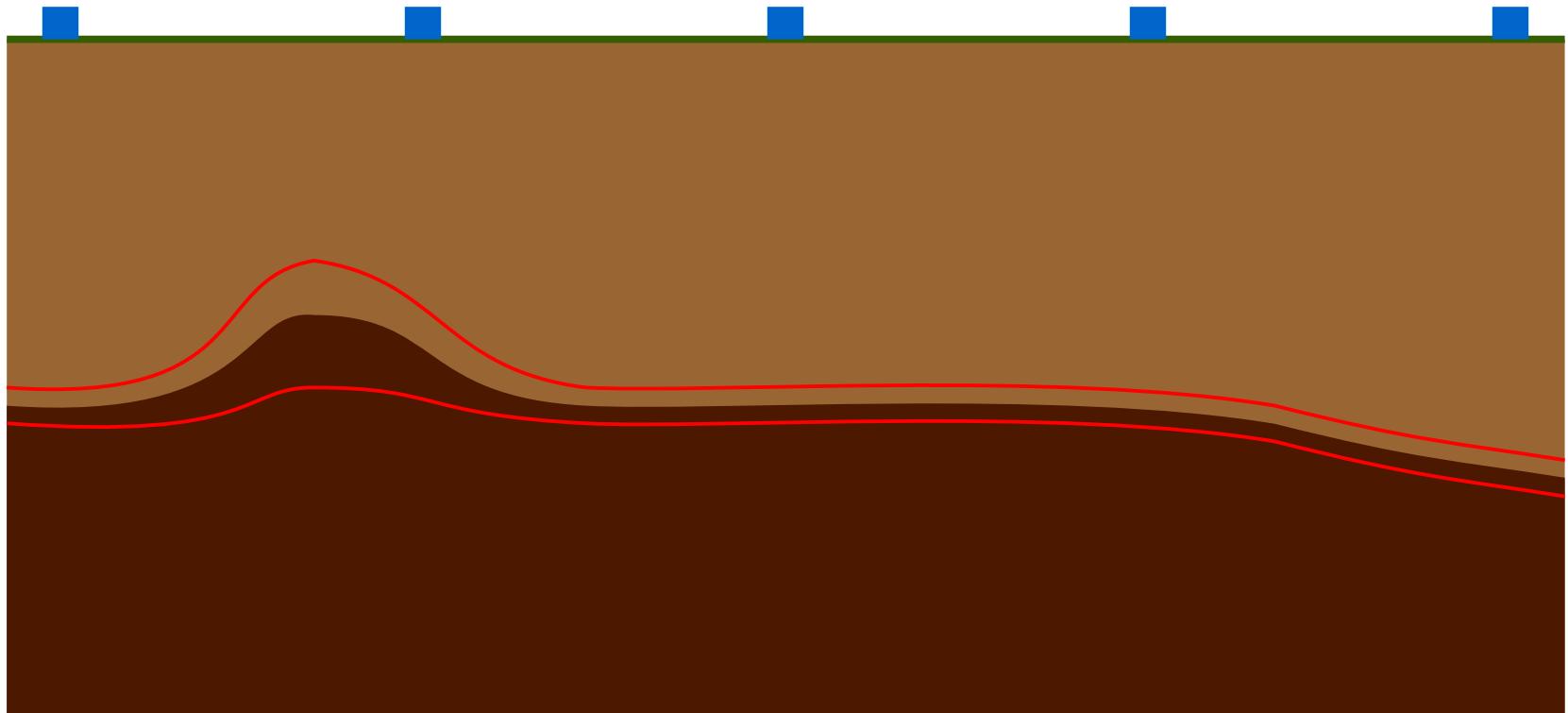
Seismic surveys



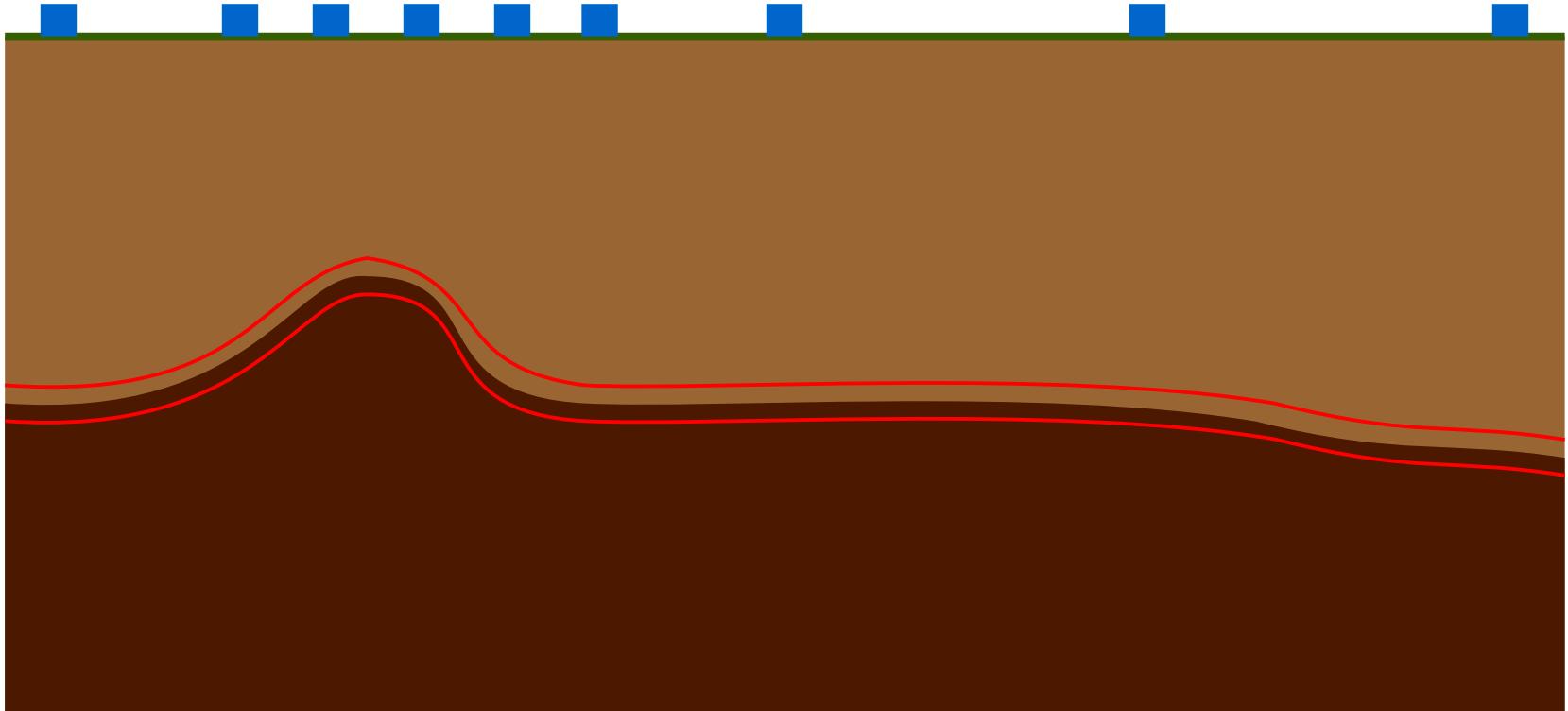
Seismic surveys



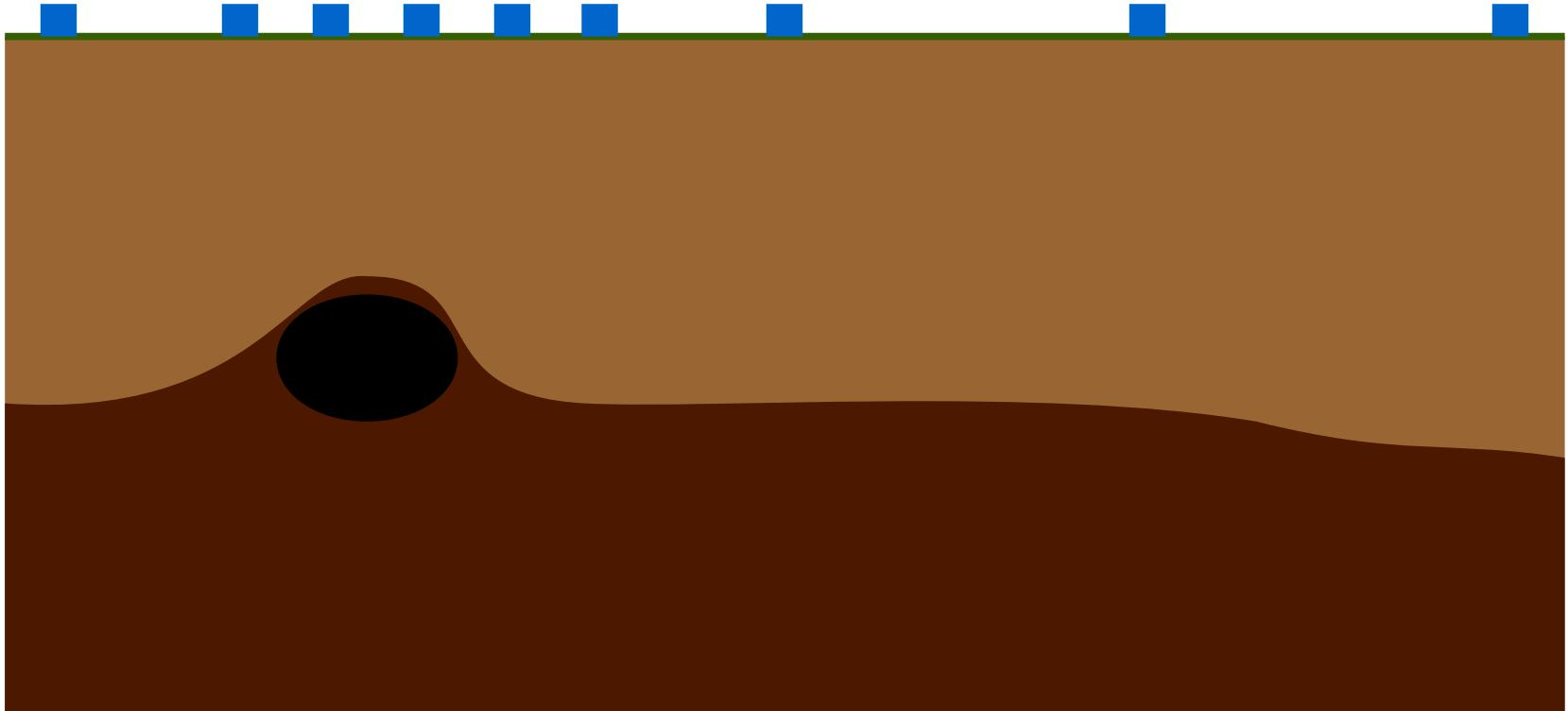
Seismic surveys



Seismic surveys



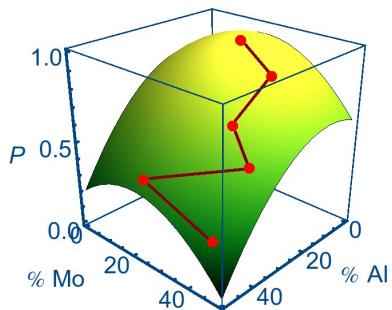
Seismic surveys



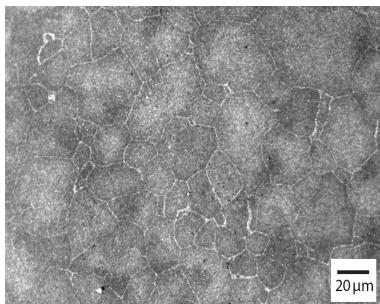
Concurrent materials design

Discovery algorithm

Patent GB1302743.8 (2013)

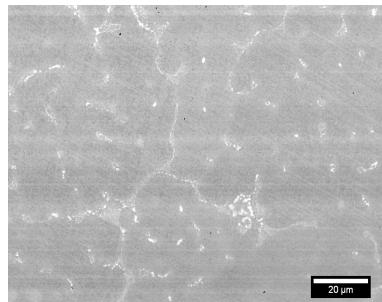


RR1000 grain growth
Acta Materialia, **61**,
3378 (2013)



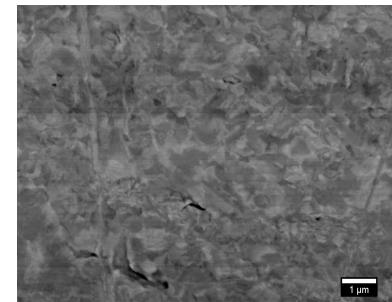
Mo-Hf forging alloy

Patent GB1307533.8 (2013)

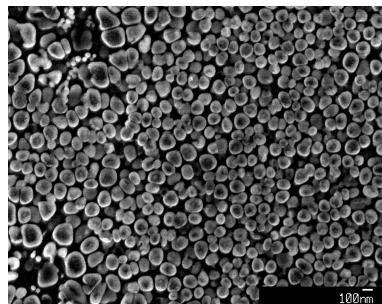


Mo-Nb forging alloy

Patent GB1307535.3 (2013)



Ni disc alloy
Rolls-Royce invention
NC12261 (2012)



Ni combustor liner
Rolls-Royce invention
NC13006 (2013)

